DAVID W TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CE--ETC F/G 13/10 PREDICTION OF THRUST-DEDUCTION AND WAKE FRACTIONS FOR TWIN-SCRE--ETC(U) AD-A092 449 NOV 80 R B HURWITZ DTNSRDC/SPD-693-02 UNCLASSIFIED NL 1052

PREDICTION OF THRUST-DEDUCTION AND WAKE FRACTIONS FOR TWIN-SCREW DESTROYERS



# DAVID W. TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER

Bethesda, Maryland 20084

PREDICTION OF THRUST-DEDUCTION AND WAKE

FRACTIONS FOR TWIN-SCREW DESTROYERS

by

RAE B. HURWITZ

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Ship Performance Department



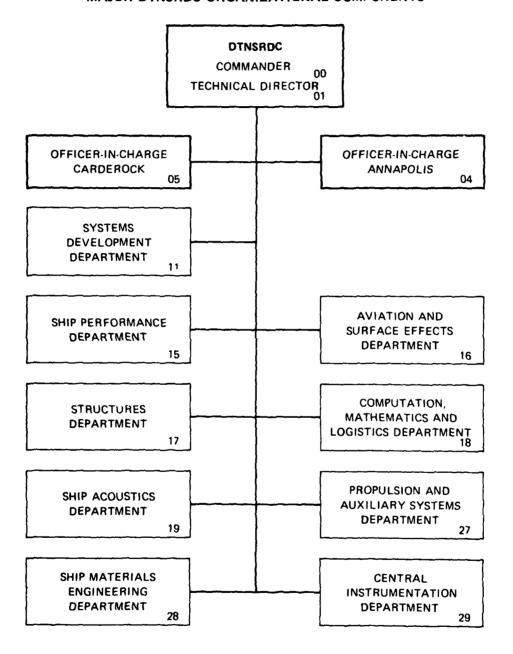
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REPORT DOCUMENTAT		READ INSTRUCTIONS BEFORE COMPLETING FORM
DTNSRDC/SPD-693-02	A N-A 19	0. 3 RECIPIENT'S CATALOG NUMBER
PREDICTION OF THRUST-DEDUCT: WAKE FRACTIONS FOR TWIN-SCRI	ION AND EW DESTROYERS	5 TYPE OF REPORT & PERIOD COVERED  9 FINAL P
7. AUTHOR(*) RAE B./HURWITZ	1	8 CONTRACT OR GRANT NUMBER(9)
PERFORMING ORGANIZATION NAME AND ADD David W. Taylor Naval Ship Ship Performance Department Bethesda, MD 20084		10 PROGRAM ELEMENT PROJECT, TASK AREA & WORK UNIT NUMBERS Program Element 62543N Task Element ZF-43-421-00.
Naval Material Command Washington, DC 20362	//	November 1980  13 Number of Pages  105 + xii
FY 11/12 11/2 11/2 17/2 17		15. SECURITY CLASS. (of this report)  UNCLASSIFIED  150. DECLASSIFICATION DOWNGRADING SCHEDULE
17 DISTRIBUTION STATEMENT (of the abatract on	tered in Block 20, if different f	rom Report)
18 SUPPLEMENTARY NOTES		
19 KEY WORDS (Continue on reverse elde if necess) Thrust-deduction fraction Thrust-wake fraction	ary and identify by block number	rr)
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#### NOTATION

 $\mathbf{A}_{\mathrm{BT}}$ Sectional area at forward perpendicular Sectional area at midships A<sub>M</sub> Disk area A<sub>O</sub> Projected blade area Ap  $A_{P}/A_{O}$ Projected area-disk area ratio  $A_{WA}$ Afterbody waterplane area Forebody waterplane area A<sub>WF</sub> Total area of waterplane  $A_{W}$ Area of maximum transverse section AX Beam or breadth, moided of a ship  $\mathbf{B}_{\mathbf{X}}$ Beam at the waterline at maximum transverse section  $B_{x}/T_{x}$ Beam-draft ratio  $C_{\mathbf{p}}$ Longitudinal prismatic coefficient  $C_{\mathbf{PA}}$ Afterbody prismatic coefficient  $^{\rm C}_{
m PE}$ Entrance prismatic coefficient  $C_{\mathbf{PF}}$ Forebody prismatic coefficient  $c_{\mathtt{PR}}$ Run prismatic coefficient  $^{\rm C}$ WP Waterplane coefficient Afterbody waterplane coefficient Forebody waterplane coefficient CWPF

#### NOTATION (CONTINUED)

D Diameter of a propeller D/T Propeller diameter-draft ratio FB Distance of longitudinal center of buoyancy from forward perpendicular FF Distance of longitudinal center of flotation from forward perpendicular  ${\tt f}_{\tt B_{\tt T}}$ Area ratio at bow; Taylor's "f" at forward perpendicular Gravitational constant i<sub>E</sub> Half angle of entrance  $J_{T}$ Advance coefficient  $J_{V}$ Ship speed advance coefficient  $K_{\mathbf{T}}$ Thrust coefficient L or L<sub>WL</sub> Total length on waterline Length of afterbody  $L_{A}$ Length of entrance  $L_{\rm E}$ Length of forebody Length of parallel middlebody  $L_{\mathbf{p}}$ Length of run  $L_{R}$  $L_{WL}/B_{X}$ Length-beam ratio Propeller pitch P P/D Pitch ratio R Resistance

# NOTATION (CONTINUED)

R<sub>n</sub> Reynolds number based on ship length S Wetted surface Froude's wetted surface coefficient (3) Т Draft, molded of a ship TH Thrust at propeller TX Draft at maximum transverse section Thrust-deduction fraction Speed of ship V/VgLW: Froude number Taylor wake fraction determined from thrust  $w_{\mathrm{T}}$ Displacement weight Scale ratio, lambda  $\triangledown$  or  $\triangledown_{\mathbf{T}}$  . Total displaced volume 7/(0.10L)<sup>3</sup> Fatness Ratio  $\nabla_{\mathbf{A}}$ Volume of afterbody  $\triangle^{\mathbf{E}}$ Volume of entrance Volume of forebody Volume of run

Kinematic Viscosity

ν

#### ABSTRACT

This work describes the development of a technique for predicting the propulsion coefficients from hull-form parameters. The two propulsive coefficients used at DTNSRDC and included in this study are the thrust-deduction fraction (t) and the thrust-wake fraction ( $w_T$ ). A prediction method has been derived from data of sixty-five experiments on model hulls representing a variety of twin-screw destroyers. Examples show that the prediction models provide fair results within the range of data represented. Additional work is recommended to develop an amproved prediction method.

#### ADMINISTRATIVE INFORMATION

The David Taylor Naval Ship R&D Center (DTNSRDC) was requested under the Ship Performance and Hydromechanics Program, sponsored by the Naval Material Command (NAVMAT 08T3), to develop a prediction method for estimating propulsor interaction coefficients. The work was funded under the Ship Performance and Hydromechanics Program and the Work Unit Number was 1500-103.

#### INTRODUCTION

The interaction between the hull and the propeller is characterized by the thrust-deduction fraction (t), and the thrust-wake fraction ( $\mathbf{w}_T$ ). It is desirable to have a reliable technique for estimating the thrust-deduction fraction and the thrust-wake fraction of twin-screw destroyers. The best method for determining these coefficients is to conduct resistance, propulsion, and open-water experiments. This is not always practical, and the naval architect must often resort to an empirical technique. This report presents a technique for estimating these interaction coefficients from hull-form parameters and propeller characteristics.

The thrust-deduction is defined as the fractional loss of thrust due to the propeller-hull interaction,

$$t = \frac{TH - F}{TH}$$

where TH is the thrust produced by the propeller and R is the towed resistance of the hull without the propeller. The thrust-deduction is usually determined by conducting conventional resistance and self-propulsion model experiments in a towing tank.

The thrust-wake fraction is the integrated velocity defect in way of the propeller. The Taylor wake fraction is deduced from experimental data obtained from an openwater experiment and a propulsion experiment with the same propeller in a towing tank. The wake fraction is determined by computing the thrust coefficient  $(K_T)$  and ship speed advance coefficient  $(J_V)$  from the propulsion experiment, and by using the open-water curve at the experimental value of  $K_T$  to get a value of advance coefficient  $(J_T)$ . The thrust-wake fraction is then determined from:

$$w_{T} = 1 - (J_{T}/J_{V}) .$$

The thrust-wake fraction and thrust-deduction fraction are dependent on many factors. Therefore, it is difficult to determine which parameters are significant. Wake is affected by hull shape, particularly just forward of the propeller location; propeller geometry, including diameter, pitch, rake, and loading; tip clearance between hull and propeller; distance of propeller tips below the free surface; size, shape, and location of appendages with respect to the propeller; and roughness of the hull surface. The variables which affect the thrust-deduction fraction are generally the same as those listed for the wake. In addition, the size and shape of the rudder and its proximity to the hull, and three propeller characteristics - diameter, radial distribution of loading, and axial position may have an effect on the thrust-deduction fraction.

In 1950, Harvald discussed techniques for estimating the thrust-wake fraction and thrust-deduction fraction of single-screw cargo ships. He evaluated twenty-one different methods used for conventional single-screw cargo ships. He determined that the methods of Taylor and Schoenherr were the best available at that time. He then presented his own method, and concluded that his method as accurate as the Schoenherr method, but easier to use. His final recommendation was to use the Taylor method if a simple technique was satisfactory, and to use his own method if more accuracy was needed.

Grant and Wilson<sup>4</sup> studied the wake and thrust-deduction for 65 twin-screw destroyers. They drew no positive conclusions and did not develop any predictive methods.

<sup>&</sup>lt;sup>1</sup>References are listed on page 10.

#### DESCRIPTION OF DATA

Three types of hull-forms were considered as prototypes for this analysis. Pata existed from model experiments at DTNSRDC for 150 models of conventional single-screw cargo ships, 65 twin-screw destroyers, and 19 single-screw destroyer escorts. It was decided to begin the analysis with the 65 twin-screw destroyers, since the prediction for this class of ships would be more relevant and useful to the naval architect designing naval combatants. Classes represented by the twin-screw destroyers included the SPRUANCE, FORREST SHERMAN, CHARLES F. ADAMS, AND MITSCHER.

An analysis of existing experimental data on twin-screw destroyers was conducted to determine the effects of twenty-four parameters on the thrust-deduction and thrust-wake fractions. The choice of these parameters was dictated by their availability. The data were correlated with various hull and propeller parameters. The twenty-four independent variables chosen for the interaction prediction model were:

- (1) Froude's wetted surface coefficient (S),
- (2) length-beam ratio  $(L_{WL}/B_X)$ ,
- (3) beam-draft ratio  $(B_X/T_X)$ ,
- (4) prismatic coefficient (Cp),
- (5) half angle of entrance (i<sub>E</sub>),
- (6) longitudinal center of buoyancy-waterline length ratio (FB/LWL),
- (7) Taylor's 'f'  $(f_{BT})$ ,
- (8) fatness ratio  $(\nabla/(0.10L)^3)$ ,
- (9) waterplane coefficient  $(C_{WP})$ ,
- (10) longitudinal center of flotation-waterline length ratio  $(\overline{FF}/L_{Wl})$ ,
- (11) length of parallel middlebody-waterline length ratio ( $L_{\rm P}/L_{\rm WL}$ ),
- (12) length of entrance-waterline length ratio ( $L_{\rm E}/L_{\rm UI}$ ),
- (13) afterbody waterplane coefficient  $(C_{\text{UPA}})$ ,
- (14) forebody waterplane coefficient (C<sub>WPF</sub>),
- (15) afterbody prismatic coefficient  $(C_{pA})$ ,
- (16) forebody prismatic coefficient (CpF),
- (17) entrance prismatic coefficient (CpE),
- (18) run prismatic coefficient (Cpp),
- (19) scale ratio  $(\lambda)$ ,
- (20) propeller diameter-draft ratio (D/T),

- (21) projected area-disk area ratio  $(A_p/A_0)$ ,
- (22) pitch ratio (P/D),
- (23) ship length Reynolds number  $(R_n)$ , and
- (24) Froude number  $(V/\sqrt{gL_{WL}})$ .

The two dependent variables were thrust-deduction fraction (t) and thrust-like fraction ( $\mathbf{w}_T$ ). A complete description of the twenty-six variables is presented in Appendix A. The twenty-six parameters from the experiments on the sixty-five models are tabulated in Appendix B.

### DESCRIPTION OF COMPUTATIONAL TECHNIQUES

Computer programs developed by the University of California for statistical analysis were used in the analysis of the twin-screw destroyer data. The means, standard deviations, maximum and minimum values were calculated for each of the twenty-six parameters for the sixty-five twin-screw destroyers. Histograms and graphs were also produced using these computer programs. Documentation of these programs is given by Dixon<sup>5</sup>.

A correlation matrix was generated for the twenty-four independent variables with the thrust-deduction and wake fractions. The correlation among the hull-form parameters provide a starting point for a statistical evaluation. The values of the correlation coefficient lie between -1 and +1. The magnitude of the correlation coefficient indicates the extent to which the variation of the independent and dependent variables are interrelated. Thus, a correlation coefficient of 0.10 would show very little functional relationship between two variables, while a correlation coefficient of 0.80 would indicate a very strong functional relationship between two variables. The sign of the correlation coefficient indicates how the dependent variable shifts with changes in the independent variable. A positive correlation coefficient indicates that the dependent variable increases along with the independent variable. Conversely, a negative correlation coefficient indicates that the dependent variable increases as the independent variable increases.

A numerical regression technique determined the significance of each independent variable in the mathematical model. A multiple stepwise regression analysis computer program was used to perform this analysis. This technique contains a built-in procedure for the elimination of redundant or superfluous independent variables from

the regression analysis.

At each stage of the stepwise procedure, the independent variable which yields the greatest improvement in the "goodness" of fit, as measured by the reduction in the standard error of the estimated dependent variable, is entered into the regression equation. Variables entered at earlier stages of the procedure are retested for significance whenever a new variable is entered. A variable may be found significant at an early stage, but may become insignificant after several other variables have entered the regression. Insignificant variables are removed at each stage, prior to the inclusion of the significant variable. Hence, the final form of the regression equation will include only those independent variables that make a significant contribution to the regression equation.

The index of determination gives an estimate of the percentage of "sum of square." variation in the dependent variable that is explained by the independent variables. The positive square root of this index of determination is called the multiple correlation coefficient.

#### PRESENTATION OF RESULTS

In general, a numerical model is built from a list of available parameters. Additional parameters can be formed by combining the basic parameters. Principal hull and propeller geometry variables were collected for this study. Originally, a linear model was used in the analysis. Other models, including the logarithmic, exponential, and squared functions of the original data were also investigated. The best results were obtained from the linear model for the thrust-deduction and from the squared model for the thrust-wake fraction.

The following statistics have been computed and tabulated for each of the 24 independent variables (hull-form coefficients) and 2 dependent variables (t and  $\mathbf{w}_T$ ) for the linear model, where  $\mathbf{X}_{ij}$  represents the i th case of the j th variable and n is the number of models:

- (1) Minimum value, Min X<sub>ii</sub>
- (2) Maximum value, Max X<sub>ij</sub>
- (3) Mean,  $\bar{X}_{j} = \frac{1}{n} \sum_{i=1}^{n} X_{ij}$
- (4) Standard deviation,  $\sigma_{j} = \sqrt{\frac{1}{n}} \sum_{i=1}^{n} (x_{ij} \overline{x}_{j})^{2}$

The minimum and maximum values, means, and standard deviations of the twenty-six parameters are presented in Table 1.

Histograms of each variable, indicating the distribution of the data, are shown in Appendix C. This graphical representation of the frequency distribution consists of vertical rectangles whose widths correspond to a definite range of independent variables and whose heights correspond to the number of models with parameters occurring within the range. In general, the distribution of models on the histograms indicate a normal distribution of each of the variables. The variation of the thrustwake with the thrust-deduction is shown in Figure 1. The fact that the data on this graph show a definite band-like pattern indicates that there is a high degree of correlation between t and  $\mathbf{w}_{\mathrm{T}}$ . This is confirmed by the fact that the correlation coefficient for these two variables is 0.707.

The variation of the twenty-four independent parameters versus the dependent variables, t and  $\mathbf{w}_T$ , is shown in graphical form in Appendix D. Each one page graph has fifty units vertically and one hundred units horizontally. The data points are automatically scaled to conform to these dimensions. These figures are presented to show the variation of the basic parameters within the range of data represented. They are not meant to reveal the degree of correlation between each parameter and the experimental data, because the scatter can be due to either the variation of other parameters or due to a weak dependency between the parameter and the data.

Correlation coefficients, between the thrust-deduction (t) and thrust-wake ( $\mathbf{w}_{T}$ ) fractions and the individual independent parameters, can be compared to assess the relative association of each parameter with t and  $\mathbf{w}_{T}$ , while ignoring the influence of the other parameters. The correlation coefficients for the linear model are shown in Table 2. Table 3 presents the correlation coefficients for the squared model.

Examples of highly correlated and poorly correlated variables of the linear model are illustrated graphically in Appendix D. For the linear and squared models,  $\overline{FB}/L_{WL}$ ,  $C_{WP}$ ,  $L_E/L_{WL}$ ,  $C_{PA}$ , and  $V/\sqrt{gL_{WL}}$ , indicate the highest correlation with t. The parameters,  $\overline{FB}/L_{WL}$ ,  $C_{WP}$ , and  $C_{WPA}$  show the highest correlation with  $w_T$ . Two of the twenty-four parameters,  $L_{WL}/B_X$  and  $C_{PE}$ , are relatively statistically uncorrelated with t; and three parameters,  $\overline{S}$ ,  $f_{BT}$ , and  $C_{WPF}$ , are poorly correlated with  $w_T$ . Although there is certainly scatter among the data plotted on the figures in Appendix D, there is an obvious trend in the data on some of the figures. This indicates a high degree of correlation between the variables. The obvious "shotgun" effect on some of the plots

in Appendix D, on the other hand, indicates poor correlation.

Upon completion of the correlation studies, sample runs of the stepwise regression program were made to determine the quality of the least squares fit to the data which could be obtained using the twenty-four independent variables to fit thank  $\mathbf{w}_T$ . After twenty-three steps (the addition of 23 variables), the program achieved maximum accuracy in predicting the thrust-deduction and thrust-wake fractions using the linear model. The resulting mathematical linear models for the thrust-deduction and thrust-wake fractions are given in Tables 4 and 5, respectively. These mathematical models for thank  $\mathbf{w}_T$  are constructed as the sum of a constant and a number of terms composed of the product of a constant and one variable.

Scale ratio and Reynolds number are included in the regression models. These independent variables are arbitrary parameters whose values can be chosen at will. They indicate that there are probably some scale effects which should be studied further.

The determination indices for the linear model with the most significant parameters were 0.7068 for the thrust-deduction fraction and 0.6763 for the thrust-wake fraction. Parameters contributing to an increase in this index for the linear model for the thrust-deduction fraction were  $C_{WPA}$ ,  $V/\sqrt{gL_{WL}}$ ,  $\lambda$ ,  $L_E/L_{WL}$ ,  $i_E$ ,  $R_n$ ,  $C_P$ , D/I, and  $C_{WPF}$ ; and for the thrust-wake fraction were  $C_{WP}$ , D/T,  $C_{PF}$ ,  $R_n$ , P/D,  $\lambda$ ,  $V/\sqrt{gI_{WL}}$ , and  $L_P/L_{WL}$ .

Due to the fair results obtained from the linear model, the square of the independent variables was used to construct a new mathematical model for predicting the wake and thrust-deduction factors. The stepwise regression program was again used to analyze the data. This squared model also produced fair results. After 22 steps, the program achieved maximum accuracy in predicting the thrust-deduction factor. Maximum accuracy in predicting the wake fraction was obtained after 23 steps. The resulting squared models for thrust-deduction and wake fraction are given in Tables 6 and 7, respectively.

The determination indices for the squared model with the most significant parameters were 0.6757 for the thrust-deduction fraction and 0.6961 for the thrust-wake fraction. The parameters contributing to an increase in the index of determination for the squared model for the thrust-deduction were  $V/\sqrt{gl_{WL}}$ ,  $C_{WP}$ ,  $\overline{FF}/L_{WL}$ ,  $L_E/L_{WL}$ ,  $A_P/A_O$ ,  $i_E$ ,  $\lambda$ , and  $R_p$ ; and for the thrust-wake fraction were  $C_{WP}$ ,  $C_{PF}$ , D/T, and P/D.

#### DISCUSSION OF RESULTS

The mathematical models which have resulted from the use of stepwise regression are certainly more complex than the simple formulas given by Taylor. However, if use is made of the computer, the method is no more complex than Harvald's method. The one thing which must be emphasized with regard to the formulas is that they are valid only for the range of independent variables for which they were derived. Any attempt to employ these formulas for a parameter value outside the domain of definition of these functions may result in erroneous and misleading results.

The question of the accuracy of the present method can only be considered by looking at the prediction errors obtained by using the method. In order to obtain such data, the regression models were used to predict the values of 1-t and  $1-w_{\rm T}$  for the 65 ships used in the analysis. Similar calculations were made using the simplified formula from Taylor. This was done in order that the performance of the regression method could be gauged relative to another method.

The results of the predictions of 1-t and 1- $w_T$ , using the regression models and Taylor's model, have been divided by the measured values of these parameters, and the resulting values have been plotted as histograms. The histograms for 1-t from the regression models and Taylor's formula are plotted on Figures 2 and 3. Similar data for 1- $w_T$  are plotted on Figures 4 and 5. These figures show the number of predictions which fall within one percent intervals of error. Values less than 1.0 indicate that 1-t or 1- $w_T$ , are under-predicted and values greater than 1.0 indicate that 1-t and 1- $w_T$  are over-predicted.

A comparison of the predictors of 1-t and 1- $w_T$ , using the regression equations and Taylor's formula given in Figures 2 through 5, shows that the regression model results resemble a normal distribution and are fairly narrow, while the results of Taylor's formula are of almost uniform height and distributed over a much wider range. Analysis of the means and standard deviations of these distributions, given in Tables 8 and 9 show that the means for all formulas, except Taylor's 1-t and 1- $w_T$ , are very close to one. This signifies that these formulas are on the average correct, except for Taylor's 1-t and 1- $w_T$  formulas. The standard deviation of Taylor's formula is more than twice that of the regression formulas. This indicates that the probability of obtaining a given accuracy of prediction is twice as high for the regression models as for Taylor's formula (assuming the means are correct).

#### CONCLUSIONS AND RECOMMENDATIONS

This investigation attempted to develop a technique for estimating the thrust-deduction and thrust-wake fractions. Data for 65 ships representing a variety of twin-screw destroyers were assembled and used in the analysis. Results of this study obtained by statistical method demonstrated that the multiple regression analysis technique does not predict these interaction coefficients for twin-screw destroyers with reasonable accuracy.

The correlation of the thrust-deduction and thrust-wake fractions with the twenty-four independent variables was unsatisfactory. The analysis revealed a relatively low correlation - below 0.5 in the majority of the parameters and often a value close to zero. The thrust-wake fraction, however, was highly correlated with the thrust-deduction fraction.

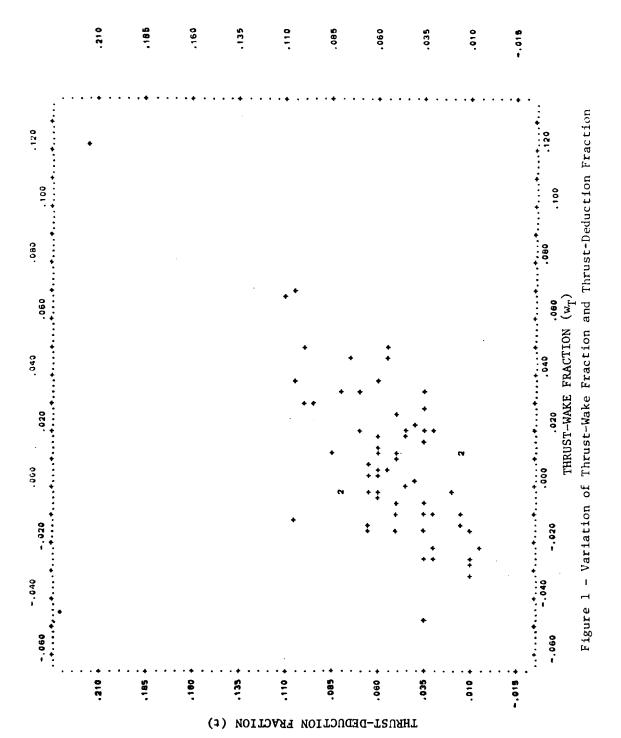
One reason for the poor estimation from this method is possibly that the method does not contain a sufficient number or type of parameters to adequately describe the variations of ship and propeller geometry within the range of data represented. No parameters representing propeller loading distribution were used, as there was insufficient information of the loading distributions for the propeller in the data sample. Addition of parameters such as the propeller tip clearance, the location of the propeller centerline relative to the ship's baseline, the size of the propeller hub compared to the propeller diameter, the size of the rudders, and propeller-to-rudder clearance might improve the prediction technique. Deletion of some parameters might also be considered.

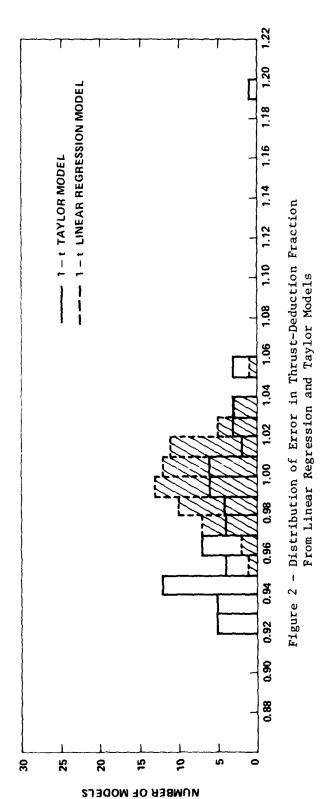
With the data available at DTNSRDC for other classes of ships, a reasonable technique might be developed utilizing common ship parameters as input to a regression analysis scheme. Further progress might be achieved by investigating other numerical models, such as the cross-products of the parameters. The results of predictions using other mathematical models or other classes of ships might satisfactorily estimate the thrust-deduction and thrust-wake fractions.

Careful statistical analysis of the data can yield significant insight into the importance of individual hull-form parameters and establish trends. Future efforts will be required to obtain a better prediction method to estimate the interaction coefficients.

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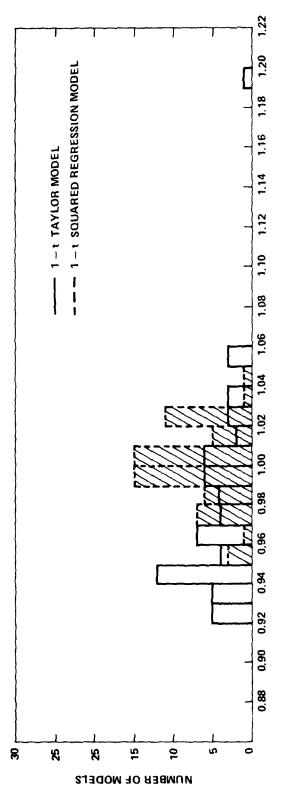
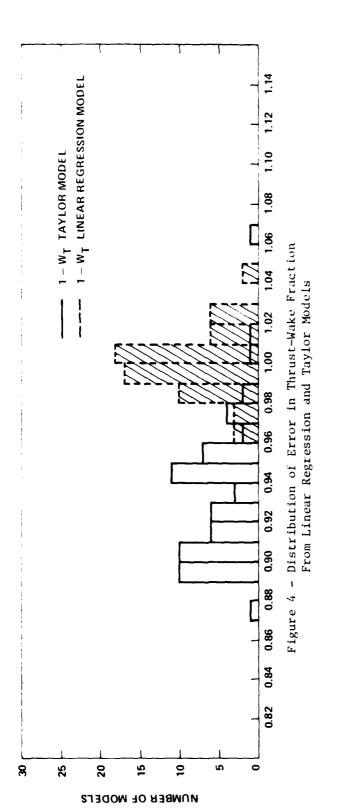


Figure 3 - Distribution of Error in Thrust-Deduction Fraction From Squared Regression and Taylor Models



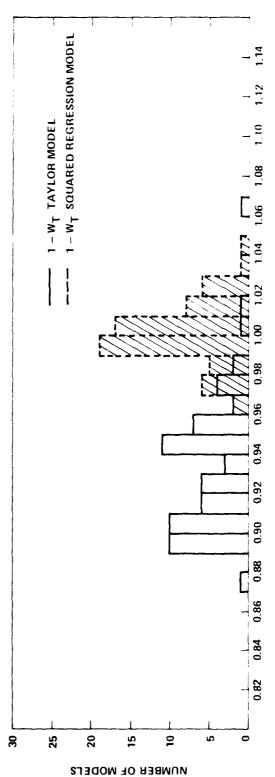


Figure 5 - Distribution of Error in Thrust-Wake Fraction From Squared Regression and Taylor Models

TABLE 1
STATISTICAL PARAMETERS FOR BASIC VARIABLES REPRESENTING
TWIN-SCREW DESTROYERS

Parameter	Minimum	Maximum	Mean	Standard
				Deviation
<b>⑤</b>	7.245	8.234	7.689	0.221
$L_{WL}/B_{X}$	8.313	10.460	9.538	0.466
$B_{\chi}/T_{\chi}$	2.717	3.650	3.171	0.192
$^{\mathrm{C}}_{\mathrm{P}}$	0.560	0.672	0.614	0.026
i <sub>E</sub>	4.000	12.000	8.126	1.967
FB/L <sub>WL</sub>	0.488	0.523	0.510	0.008
f <sub>BT</sub>	0.000	0.600	0.120	0.166
$\nabla/(0.10L)^3$	1.358	2.154	1.756	0.222
$c^{Nb}$	0.681	0.775	0.742	0.022
FF/L <sub>WL</sub>	0.514	0.588	0.559	0.015
$_{ m L_P/L_{WL}}$	0.000	0.036	0.006	0.013
L <sub>E</sub> /L <sub>WL</sub>	0.498	0.555	0.533	0.017
C <sub>WPA</sub>	0.713	0.962	0.875	0.047
$^{\mathrm{C}}$ WPF	0.559	0.694	0.618	0.032
$^{\mathrm{C}}_{\mathrm{PA}}$	0.593	0.717	0.650	0.027
$^{\mathrm{C}}_{\mathrm{PF}}$	0.531	0.660	0.587	0.030
$^{\mathrm{C}}_{\mathrm{PE}}$	0.557	0.682	0.609	0.026
c <sub>PR</sub>	0.541	0.693	0.616	0.029
λ	13.000	26.000	20.502	3.586
D/T	0.732	1.141	0.933	0.096
A <sub>P</sub> /A <sub>O</sub>	0.461	0.816	0.674	0.070
P/D	0.892	1.457	1.106	0.105
$R_{\rm n} \times 10^{-9}$	0.948	2.291	1.817	0.331
V/JgLWL	0.352	0.586	0.477	0.067
t	0.003	0.215	0.054	0.033
$\mathbf{w}_{\mathbf{T}}$	-0.049	0.121	0.009	0.028

TABLE 2

CORRELATION COEFFICIENTS FOR LINEAR VARIABLES

Parameter	t	<sup>₩</sup> T
<b>(S)</b>	0.115	-0.000
L <sub>WL</sub> /B <sub>X</sub>	-0.007	0.198
$B_{X}/T_{X}$	-0.082	-0.189
$c_{\mathbf{p}}$	-0.073	-0.025
i <sub>E</sub>	-0.298	-0.189
FB/L <sub>WL</sub>	-0.375	-0.356
f Br	0.177	0.023
∇/(0.10L) <sup>3</sup>	-0.050	-0.156
CWP	-0.355	-0.491
FF/L <sub>WL</sub>	-0.138	-0.332
L <sub>P</sub> /L <sub>WL</sub>	-0.210	-0.173
L <sub>E</sub> /L <sub>WL</sub>	-0.402	-0,308
CWPA	-0.292	-0.479
C <sub>WPF</sub>	-0.111	0.014
C <sub>PA</sub>	-0.381	-0.313
c <sub>PF</sub>	0.135	0.188
$c_{PE}$	-0.004	0.090
C <sub>PR</sub>	-0.062	-0.070
λ	0.320	0.095
D/T	-0.330	-0.330
A <sub>P</sub> /A <sub>O</sub>	-0.104	-0.189
P/D	0.058	0.065
$R_n \times 10^{-9}$	0.022	-0.106
V/√gL <sub>WL</sub>	-0.405	-0.274
t		0.707

TABLE 3

CORRELATION COEFFICIENTS FOR SQUARED VARIABLES

COMMENTATION	COLITICIENTS TON EQUINAL	VIII(2112) 22.0
Parameter	t	$^{w}_{\mathrm{T}}$
<b>S</b>	0.113	-0.003
$L^{M\Gamma}/B^{X}$	0.002	0.202
B <sub>X</sub> /T <sub>X</sub>	-0.078	-0.184
c <sub>p</sub>	-0.073	-0.025
i <sub>E</sub>	-0.277	-0.181
FB/L <sub>WL</sub>	-0.377	-0.356
f <sub>Br</sub>	0.089	-0.028
♥/(0.10L) <sup>3</sup>	-0.030	-0.149
C <sub>WP</sub>	-0.347	-0.484
FF/L <sub>WL</sub>	-0.124	-0.321
L <sub>P</sub> /L <sub>WL</sub>	-0.210	-0.173
L <sub>E</sub> /L <sub>WL</sub>	-0.401	-0.306
CWPA	-0.264	-0.460
CWPF	0.105	0.017
C <sub>PA</sub>	-0.380	-0.313
$^{\mathrm{C}}_{\mathrm{PF}}$	0.137	0.190
$^{\mathrm{C}}_{\mathrm{PE}}$	-0.005	0.088
C <sub>PR</sub>	-0.059	-0.068
λ	0.333	0.098
D/T	-0.323	-0.321
A <sub>P</sub> /A <sub>O</sub>	-0.107	-0.193
P/D	0.064	0.073
$R_n \times 10^{-18}$	0.044	-0.075
V/√gL <sub>WL</sub>	-0.398	0.276
t		0.707

TABLE 4 LISTING OF COEFFICIENTS FOR LINEAR REGRESSION MODEL FOR THRUST-DEDUCTION FRACTION (Constant (4.62328))

Step Number	<u>Variable</u>	Coefficient
1	V/√gL <sub>WL</sub>	-0.23790
2	$^{ m C}_{ m WPA}$	-1.04237
3	λ	0.00935
4	R <sub>n</sub>	-0.09146
5	$^{\mathrm{C}}_{\mathrm{P}}$	-5.35383
6	i <sub>E</sub>	-0.00507
7	D/T	-0.10526
8	∇/(0.10L) <sup>3</sup>	-0.18314
9	$c_{\overline{WP}}$	3.26399
10	$^{ m C}_{ m WPF}$	-2.10433
11	$c_{ t PF}$	-3.91022
12	f BT	-0.08448
13	P/D	-0.01213
14	${^{ m L}_{ m P}}/{^{ m L}_{ m WL}}$	0.19808
15	$B_{X}/T_{X}$	-0.01470
16	<b>S</b>	-0.06031
17	$A_p/A_0$	0.06016
18	A <sub>P</sub> /A <sub>O</sub> FB/L <sub>WL</sub> C <sub>PA</sub>	0.14966
19	$^{\mathrm{C}}_{\mathrm{PA}}$	3.09229
20	c <sub>pe</sub>	7.10020
21	$^{ m L}_{ m E}/^{ m L}_{ m WL}$	-5.08389
22	$^{\mathrm{L}}$ WL $^{/\mathrm{B}}$ X	-0.03141
23	FF/L <sub>WL</sub>	-2.80978
	17	. 1

TABLE 5
LISTING OF COEFFICIENTS FOR LINEAR REGRESSION MODEL
FOR THRUST-WAKE FRACTION
(Constant (-2.00197))

(Constant (-2.00197))		
Step Number	Variable	Coefficient
1	$c_{\overline{WP}}$	-1.94003
2	D/T	-0.12594
3	$^{\mathrm{C}}_{\mathrm{PF}}$	-1.57986
4	R <sub>n</sub>	-0.06369
5	P/D	0.04278
6	$v/\sqrt{gL_{WL}}$	-0.07447
7	$^{\mathrm{L}_{\mathrm{WL}}/\mathrm{B}_{\mathrm{X}}}$	0.03678
8	λ	0.00482
9	$^{ m L_{ m P}/L_{ m WL}}$	0.02936
10	$^{ m C}_{ m WPF}$	1.83502
11	$\mathtt{c}_{\mathtt{PE}}$	1.72391
12	$A_{P}/A_{O}$	0.03560
13	$^{ m L}{_{ m E}}^{/ m L}{_{ m WL}}$	-0.83611
14	FF/L <sub>WL</sub>	4.64832
15	$^{ m C}_{ m WPA}$	-0.52694
16	$^{\mathrm{C}}_{\mathrm{PA}}$	0.15639
17	$\mathtt{f}_{\mathtt{BT}}$	~0.01121
18	<b>S</b>	0.02383
19	$\nabla/(0.10L)^3$	0.06829
20	${}^{\mathrm{B}}\mathrm{_{X}}/{}^{\mathrm{T}}\mathrm{_{X}}$	0.02339
21	B <sub>X</sub> /T <sub>X</sub> FB/L <sub>WL</sub>	-0.50293
22	i <sub>E</sub>	-0.00018
23	C <sub>PR</sub>	0.04754

TABLE 6
LISTING OF COEFFICIENTS FOR SQUARED REGRESSION MODEL
FOR THRUST-DEDUCTION FRACTION
(Constant (0.24509))

Step Number	<u>Variable</u>	Coefficient
1	$^{ m L}_{ m E}/^{ m L}_{ m WL}$	0.02958
2	i E	-0.00022
3	$A_{P}/A_{O}$	0.01583
4	V/VgLWL	-0.21889
5	FF/L <sub>WL</sub>	-0.18688
6	λ	0.00030
7	R <sub>n</sub>	-0.03038
8	D/T	-0.05969
9	$^{\mathrm{C}}_{\mathrm{P}}$	1.17300
10	∇(0.10L) <sup>3</sup>	0.01372
11	L <sub>P</sub> /L <sub>WL</sub>	7.67789
12	$B_{X}/T_{X}$	0.01268
13	$^{\mathrm{L}}_{\mathrm{WL}}/^{\mathrm{B}}\mathrm{_{X}}$	0.00286
14	${\sf f}_{\sf BT}$	-0.09411
15	$^{C}_{WPF}$	0.02902
16	$^{\mathrm{C}}_{\mathrm{PA}}$	-0.17861
17	$c_{p_{F}}$	-0.86020
18	FB/L <sub>WL</sub>	-1.67830
19	P/D	-0.00631
20	<b>S</b>	-0.00090
21	$^{ m C_{WP}}$	-0.07393
22	$^{ m C}_{ m WPA}$	-0.03500

TABLE 7

LISTING OF COEFFICIENTS FOR SQUARED REGRESSION MODEL

FOR THRUST-WAKE FRACTION

(Constant (1.91713))

a. v 1		0661-4.
Step Number	<u>Variable</u>	Coefficient
1	$c_{ m WP}$	-0.67262
2	$c_{\mathbf{PF}}$	-5.32083
3	D/T	-0.06741
4	$R_{\mathbf{n}}$	-0.01450
5	P/D	0.01381
6	$V/\sqrt{gL_{WL}}$	-0.08095
7	$L_{WL}/B_{X}$	0.00081
8	λ	0.00011
9	$\mathtt{f}_{\mathtt{BT}}$	-0.07827
10	$c_{\mathtt{pE}}$	9.76818
11	${\tt L_p}/{\tt L_{\widetilde{\sf WL}}}$	-5.86386
12	$c_{\mathtt{WPF}}$	0.53347
13	FF/L <sub>WL</sub>	1.13789
14	${\tt L_E/L_{WL}}$	-7.73494
15	$A_{P}/A_{O}$	0.03523
16	∇/(0.10L) <sup>3</sup>	0.00752
17	<b>S</b>	0.00107
18	$B_{X}/T_{X}$	-0.00023
19	$^{C}_{WPA}$	-0. 09262
20	$C_{\mathbf{p}}$	-7.91557
21	C <sub>PA</sub>	3.92659
22	FB/L <sub>WL</sub>	-1.52020
23	i <sub>E</sub>	0.00003

TABLE 8

STATISTICAL VALUES FOR ERROR DISTRIBUTION OF THRUST-DEDUCTION AND THRUST-WAKE FRACTIONS USING LINEAR REGRESSION MODEL

PARAMETER	MEAN	STANDARD DEVIATION
(1-t) Predicted (1-t) Experimental	1.0004	0.0193
(1-t) Taylor (1-t) Experimental	0.9790	0.0449
$\frac{(1-w_T) \text{ Predicted}}{(1-w_T) \text{ Experimental}}$	1.0003	0.0162
$\frac{(1-w_T)}{(1-w_T)}$ Taylor Experimental	0.9336	0.0350

TABLE 9
STATISTICAL VALUES FOR ERROR DISTRIBUTION OF
THRUST-DEDUCTION AND THRUST-WAKE FRACTIONS
USING SQUARED REGRESSION MODEL

PARAMETER	MEAN	STANDARD DEVIATION
(1-t) Predicted (1-t) Experimental	1.0000	0.0202
(1-t) Taylor (1-t) Experimental	0.9790	0.0449
(1-w <sub>T</sub> ) Predicted  (1-w <sub>T</sub> ) Experimental	1.0010	0.0159
$\frac{(1-w_T) \text{ Taylor}}{(1-w_T) \text{ Experimental}}$	0.9336	0.0350

## TABLE A-1

DESCRIPTION OF INDEPENDENT AND DEPENDENT VARIABLES

1. (S) Froude's Wetted Surface Coefficient

$$\mathbf{\hat{S}} = \frac{\mathbf{S}}{\nabla_{\mathbf{T}}^{2/3}} ,$$

where S is wetted surface and  $\boldsymbol{\triangledown}_{T}$  is total displaced volume

2.  $\frac{L_{WL}}{B_{y}}$  Length-Beam Ratio,

where  $\mathbf{L}_{WL}^{}$  is waterline length and  $\mathbf{B}_{X}^{}$  is maximum beam at waterline

3.  $\frac{B_X}{T_X}$  Beam-Draft Ratio, where  $B_X$  is maximum beam and  $T_X$  is maximum draft

4.  $C_{p}$   $C_{p} = \frac{\nabla T}{L_{tot} A_{y}}$ Prismatic Coefficient,

where  $\nabla_{_{\hbox{\scriptsize T}}}$  is total displacement volume,  $L_{_{\hbox{\scriptsize WL}}}$  is waterline length, and  $A_{_{\hbox{\scriptsize X}}}$  is maximum section area

- 5.  $i_{E}$  Half Angle of Entrance in degrees, of waterline at bow with reference to centerplane
- 6. FB/L<sub>WL</sub>

Ratio of longitudinal center of buoyancy from forward perpendicular to waterline length

7.  $f_{\mbox{\footnotesize{BT}}}$  Taylor sectional area coefficient for bulbous bow

$$f_{BT} = \frac{A_{BT}}{A_{\chi}}$$

Ratio of sectional area curve at FP to sectional area at maximum section

8.  $\nabla/(0.10L)^3$  Fatness Ratio

where displaced volume  $(\nabla)$  is for salt water and length is on the waterline

9.  $C_{WP}$  Waterplane Coefficient  $C_{WP} = \frac{A_{W}}{L_{WI, B_{X}}}$ 

where  $\boldsymbol{A}_{\widetilde{W}}$  is total waterplane area,  $\boldsymbol{L}_{\widetilde{WL}}$  is waterline length, and  $\boldsymbol{B}_{\mathbf{v}}$  is maximum beam at waterline

- 10.  $\overline{\text{FF}}/L_{\overline{WL}}$ , Longitudinal center of flotation aft of Forward Perpendicular, as fraction of length on waterline
- 11.  $L_p/L_{WL}$ , Length of parallel middlebody as fraction of waterline length
- 12.  $L_E/L_{WL}$ , Length of entrance as fraction of waterline length
- 13. CWPA Afterbody Waterplane Coefficient

$$C_{WPA} = \frac{A_{WA}}{L_A B_X}$$

where  ${\bf A_{WA}}$  is the waterplane area of the afterbody,  ${\bf L_A}$  is one-half of  ${\bf L_{WL}}$  or length of the afterbody, and  ${\bf B_X}$  is maximum beam at the waterline

14.  $C_{WPF}$  Forebody Waterplane Coefficient

$$C_{WPF} = \frac{A_{WF}}{L_F B_X}$$

where  ${\bf A_{\rm WF}}$  is the waterplane area of the forebody,  ${\bf L_{\rm F}}$  is one-half of  ${\bf L_{\rm WL}}$  or length of the forebody, and  ${\bf B_{\rm X}}$  is maximum beam at waterline

15.  $C_{p_A}$  Afterbody Prismatic Coefficient

$$C_{PA} = \frac{\nabla_A}{L_A A_M}$$

where  $\mathbf{L_A}$  is one-half of  $\mathbf{L_{WL}}$  or length of the afterbody,  $\nabla_{\mathbf{A}}$  is volume of the afterbody and  $\mathbf{A_M}$  is midship-section area

16. C<sub>pp</sub> Forebody Prismatic Coefficient

$$C_{PF} = \frac{\nabla_F}{L_F A_M}$$

where  $\mathbf{L_F}$  is one-half of  $\mathbf{L_{WL}}$  or length of the forebody,  $\mathbf{\nabla_F}$  is volume of the forebody, and  $\mathbf{A_M}$  is midship-section area

17.  $C_{p_F}$  Entrance Prismatic Coefficient

$$C_{PE} = \frac{\nabla_{E}}{L_{E} \Lambda_{X}}$$

where  $\mathbf{L}_E$  is the length of entrance,  $\boldsymbol{\nabla}_E$  is the volume of entrance, and  $\mathbf{A}_{\mathbf{X}}$  is maximum section area

18. C<sub>pp</sub> Run Prismatic Coefficient

$$C_{PR} = \frac{\nabla_R}{L_p A_v}$$

where  $\mathbf{L}_R$  is the length of run,  $\nabla_R$  is the volume of run, and  $\mathbf{A}_{\mathbf{X}}$  is maximum section area

19.  $\lambda$  Scale Ratio

Length of ship to length of model scale ratio

20. D/T Propeller Diameter - Draft Ratio

Ratio of ship propeller diameter to ship draft

21.  $A_p/A_0$  Projected Area - Disk Area Ratio

Projected area ratio of blades of propeller (outside of hub) to disk area

22. P/D Pitch Ratio

Ratio of propeller pitch to propeller diameter

23. R Ship Length Reynolds Number

$$R_{n} = \frac{V \cdot L_{WL}}{(\nu)}$$

where V is design speed, and  $L_{WL}$  is length of waterline, and  $\nu$  is kinematic viscosity of salt water at  $59^{\circ}F$ 

24.  $V/\sqrt{gL_{WL}}$  Froude number

Design speed divided by the square root of the gravitational acceleration and length on the waterline

- 25. t Thrust-deduction fraction
- 26.  $\mathbf{w}_{\mathrm{T}}$  Taylor wake fraction determined from thrust identity

	<del></del>									[				Ĭ	
<b>③</b>	L/B	B/T	c <sub>p</sub>	t <sub>E</sub>	न्ह्र/1 <sub>vn</sub> _	f <sub>BT</sub>	2 - L	€ <sub>WP</sub>	FF LWL	L <sub>p</sub> /L	L <sub>E</sub> /L	C <sub>™PA</sub>	C <sub>₩PF</sub>	PA	P
.682	19.175	3.357	0.628	9.0	0.497	0.0	38.79	0.681	0.514	5.5	0.505	··. *13	1.45	1,42*	
.682	10.175	3. 157	0.628	9.0	0.497	0.0	38.79	0.681	0.514	0.6	6.565	9,713	3.832	2.62*	
.587	9,794	3.344	0.616	8.5	0.515	0.0	46.37	0.740	0.549	0.0	9.559	9,893	0.611	0.651	
. 587	9.794	3.344	0.616	8.5	0.515	0.0	46.17	0.740	0.549	0.0	0.559	5.851	5.631	1.01	
.923	10.132	3.263	0.592	7.0	0.514	0.0	40.85	0.741	6.557	0.0	0.550	0.871	1.622		
. 720	9.569	3.284	0.594	8.5	0.513	0.02	45.78	0.735	0.556	0.0	0.550	9.870	14.04.	3,963	
.918	10.309	3.20R	0.600	9.0	9.513	0.02	41.43	0,752	0.560	1.0	0.550	G.879	0.621		
.717	9.541	3.155	0.600	9.0	0.515	0.04	48,86	0.741	0.556	0.0	0.550	6.874	9.628		
.717	9.541	3.155	0.600	9.0	0.515	0.04	48.86	0.741	0.556	0.5	0.550	0.876	C.628	1,43%	
.717	9.541	3.155	0.600	0.0	0.515	0.04	48.86	0.741	0.556	0.0	0.556	0.876	1.638	1.635	
.662	9.524	3.111	0.617	9.0	0.516	0.02	50.22	0.750	0.560	0.0	0.550	5.887	6.622	),464	
.662	9.524	3.111	0.617	9.0	0.516	0.02	50,22	0.750	0.560	0.0	C.550	3,687	0.6.2	204	
.771	9.785	3.650	0.643	12.0	0.500	0.00	41.92	0.763	0.537	0.0	0.506	0.941	0.683	3.5m	
.626	9.985	3.497	0.672	12.0	0.509	0.001	46.94	0,775	0.538	0.0	0.500	0.856	0.694		
.417	9.050	3.135	0.618	9.5	0.519	0.000	57.28	0.748	0.560	0.0	0.525	7.88-	0.623	9,646 3,679	
.482	9,453	3.117	0.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	9.530	ა.გგ9	7.633	1	
.482	9,453	3.117	0.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	0.530	0.689	0.63;	19,679	
.482	9.453	3.117	0.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	0.530	0.889	0.633	2.879	
.482	9.453	3.117	0.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	0.530	9.889	3.613	2,674	
.482	9.453	3.117	9.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	0.530	0.889	.633	/, m <sup></sup> 4	
. 482	9,453	3.117	0.633	9.5	0.518	0.028	54.30	0.758	0.560	0.036	0.530	J.889	0.611	7,6**	
.482	9,453	3,117	0.631	4.5	0.518	0.028	54.30	0.738	0.560	0.036	0.530	0.889	0.633	1,579	
.482	9,453	3.117	0.613	9.5	0.518	0.028	54.30		0.560	0.634	0.530	0.889	0.633		
. 296	9.105	3.090	0.614	9.5	0.519	0.020	57.13	0.752	0.561	0.000	0.555	0.889	0.625	9,671	
. 324	10.138	2.834	0.627	8.5	0.500	0.000	48.99	0.692	0.520	0.000	0.499	0.734	9.649	1,631	
. 365	10.460	2.717	0.646	10.0	0.523	0.000	47.56	0.755	0.551	0.000	0.547	0.883	0.652	1.717	
276	9.095	3.374	0.549	11.0	0.513	0.000	57.36	0.773	0.544	0.000	0.525	0.866	0.683	3,682	
.779	10.162	3.088	0.629	4.0	0.509	0,010	46.85	0,751	0.549	0.000	0.513	0.858	0.650	0.657	
.726	9,690	3.148	0.611	8.0	0.515	0.030	47.26	0,725	0.562	0.000	0.550	0.863	0.599	.,661	
.825	9.662	3.000	0.572	5.6	0.505	0.054	47.00	0.703	0.566	0.000	0.522	0.849	0.565	0.593	
.812 .917	9.934 9.934	3.423 3.423	0.633	8.5 8.5	0.516	0.023 0.480	41.50 43.01	0.743 0.741	0.559	0.000	0.547	0.887 0.885	0.620	0.663 0.663	
														}	
.959 .311	9.434 9.148	3,423 3,946	0.654	8.5 12.0	0.4#8 0.515	0.60 0.00	44.42 57.71	0.742	0.560	0.0	0.547	0.885 0.882	0.619 0.659	0.663	
.48Z	9.453	3.117	0.633	9,5	0.515	0.028	54.30	0,758	0,560	0.036	0.530	0.889	0.633	1,516	
.815	9.453	3.117	0.667	9.5	0.316	0.39	57.13	0.758	0.560	0.036	0.530	0.889	0.633	0.679	
-925	9.839	3.162	0.560	4.0	0.440	0.00	40,54	0.712	0.570	0.0	0.537	0.875	0.573	0.603	
.141	9.819	3.162	0,564	4.0	0.512	0.17	40.82	0.712	0.570	0.0	0.537	0.875	0.5"3	0,603	c
.009	9.735	3.145	0,561	5.5	0.515	0.0	40.61	0.711	0.571	0.0	0.517	0.876	0.568	0.605	,
. 245	8,430	3.135	0.636	10.75	0.509	0.0	60.67	0.765	0.551	0.0	0.518	0.873	0.658	0.657	
. 382	8.930	3 1 **	0.044	10.75	0.503	0.26	61.43	0,765	0.551	0.0	0.518	0.873	0.658	0.657	
.382	9,524	3.135	0.585	6.00	0.507	0.07	45.52	0.724	0.567	0.0	0.500	0.872	0.577	0.604	, س
.754	9.624	3.210	0.587	4.50	0.506	0.19	48.04	0.724	0.574	0.0	0.550	0.897	0.575	0.604	,
921	9.495	3.074	0.594	4.50	0.501	0.33	48.60	9.724	0.574	0.0	0.550	0.897	0.575	0.614	,
.537	9.450	2,891	0.694	5.50	0.521	0.0	52.39	0.737	0.567	0.0	0.525	0.894	0.598	0.65	
.762	9.650	2.891	0.617	5.50	0.511	0.33	\$3,50	0.737	9,567	0.0	0.525	0.894	0.598	1).654	
.616	9,506	2.807	0.629	5.50	0.505	0.30	57.99	0.754	0.569	9.0	0.518	0.907	0.610	0.543	
700	9.545	3.066	0.574	4.50	0.501	0.26	49.85	0.734	0,561	0.0	0.51-	0.880	0.608	0.594	
234	9.847	3.505	0.644	6.5	0.489	0.58	44.23	0.741	0,575	0,0	0.544	0.931	0.586	0.655	
670	9,494	2.928	0.614	6.6	0.503	0.28	53.90	0.756	0,567	9.0	0.525	0,903	0.616	0.630	,
742	8.607	3.342	0,573	1.0	0.517	0.283	54.96	0.710	0.573	0.0	0.150	0.884	0.564	0.642	
986	9.722	1.000	0,562	5.5	0.501	0.33	46.51	0.724	0.579	0.0	0.550	0.901	0.559	0,597	
129	8.600	3.242	0.615	7.9	0.500	0.48	59.44	0.768	0.588	0.0	0.525	0.962	0.580	0.640	
904	8,585	3.128	0.607	7.0	0.513	0.34	61.53	0.771	0.587	0.0	0.525	0.960	0.583	3,649	
904	8.385	3.128	0.607	7.0	0.513	0.14	61.53	0.771	0.587	0.0	0.525	0.960	0.583	J. 544	-
900	8.333	3.503	0.592	6.5	0.501	0.32	55.28	0.724	0,566	0.0	0.590	0.861	0,586	17.606	,
748	9.055	3.017	0.633	9.9	0.514	0.30	59.08	0.167	0,571	a.u	0.550	0.931	0.618	0.613	
867	9.440	2.821	0.575	7.0	0.512	0.29	52.46	0.736	0.582	0.0	0.550	0.917	0.362	0.628	
.867	4.640	2.821	0.575	7.0	0.512	0.29	52.48	0.736	0,582	0.0	0.550	0.917	0.562	0.628	(
.632	9.213	3.155	0.676	A.0	0.515	0.0	52.28	0.255	0.562	0.0	0.525	0.883	0.628	0.659	•
. 647	8.313	3.609	0.615	10.0	9.515	0.025	56.71	12.718	0.556	0,0	0.550	0.873	0.622	0.654	,
. 549	10.119	3.278	0.625	9.0	D. 498	0,0	40.51	9.681	0.515	0.0	0.498	0,713	0.650	0.622	ť
. 587	9.794	3.346	0.616	0.5	0.515	0.9	46.37	9.740	0.544	0.0	0.550	0.813	0.611	0.561	c
.597 .923	9,794	3.344	0.616	8.5	0.515	0.0	46.1"	9.740	0.549	0.0	0.550	0.853	0.631	0.661	0
	10.112	3.243	0.592	1.0	0.514	9.0	40,85	0.741	0.557			0.871	0.622	0.641	0

 $\begin{tabular}{llll} TABLE & B-1 \\ \\ SUMMARY & OF & MODEL & PARTICULARS & AND & BASIC & PARAMETERS \\ \end{tabular}$ 

					)			Ap/An		Ship Reynolds	VAT.	,	
G <sub>LPA</sub>	CWPF	C <sub>PA</sub>	C <sub>PF</sub>	C <sub>PE</sub>	C <sub>PR</sub>	SCALE.	<u>0/7</u>	-	P/D	Number x 10 - 7			Ť
0.713	0.650	0.627	0.630	0.633	0,623	15-5	0.9840	0.395	1.192	1.2286	1.791	9 117	0,067
0.713	0.650	0.627	0.630	0.633	0.623	15.5	1.0489	0.608	1.700	1.2286	1.701	1.0	(,975
0.853	0.631	0.661	0.576	0.612	9,620	16.7	1.0780	u. <b>67</b> 0	1.090	1.5834	1.970	0,040	-6.022
0.853	0.631	0.661	0.576	0.612	0.620	16.7	1.0786	0.638	1.090	1.5834	1,976	0.612	-0.726
0.871	0.622	0.641	0.544	0.594	0.590	18.6	0.4218	0.630	1.170	1.7445	1.81'	. 29	-0.02 <b>6</b>
9.870	0.520	0.643	0.565	0.595	0.592	16.	1.0583	0.680	1.100	1.519-	1.915	5.515	-5.028
0.879	0.621	0.647	0.584	0.601	0. <b>50</b> 0	18.6	1.0000	0.685	1.076	1.7645	1.867	0.044	-0.916
G.874	0.629	0.655	0.572	0.599	0,602	16.7	0.9845	0.634	1.0974	1.7854	1.548	0.40	>0.016
			0 172	0.640	9,602	16.7	1.0066	0.655	1.055	1.2854	1.548	9.036	0.015
0.876	0.628	0.655		0.549	0.602	16.7	1.0066	0.655	1.055	1.78%	1.348	0.034	9.011
0.876	0.628	0.655	0.572	0.599	1	18.45	0.9020	0.726	1.068	1.7907	1.822		0.022
0.887	0.622	0.669	0.579	0.611	0.625	18.45	0.9237	0.747	1.0797	1.7007	1.822	0.001	-0.022
U.887	0.622	0.669	0.579	0.611	0.625	17.40	1.0769	0.624	1.254	1.649	1.936	2.060	0.012
0.841	0.685	0.647	0.650	0.650	0,693	18.20	0.9856	0.711	1.276	1.7505	1.913	0.060	0.006
3.856	0.694	3,694				18.45	0.9231	0.686	1.042	1.6521	1.770	4,031	2.020
0.88.	0.623	0.668	0.574	0.542	0.648	18.45	0.9423	0.589	1.027	1.7148	1.712	0.039	0.001
0.889	0.633	0.874	7.766	0,012	0.017				****		•••		0.001
	2.622	0.670	0.306	0.412	ا مده	10 /6	0.9231	0.700	1.070	1.7148	1 717		0.017
0.889	0.631	0.679	0.388	0.612	0.6.9	18.45 18.45	1.0346	0.700	1.200	1.7148	1.737	0.045	0.017
0.889	0.633	0.679		0,612	i	1	1.0385	0.765		1.7148		0.037	-0.007
2.889	0.633 0.631	0.679 0.679	0.588 0.588	0,612	0.629	18.45 18.45	1.1408	0.665	1.043	1.7148	1.737	0.016	-0.015
986.0		l .	0.588	0.612		18.45	0.9423	0.589	1.027		1.737	0.015	-0.01
3.889	0.633	0,679		0.612	0.629			0.700		1.7148	1.737	0.016	0.011
0.889	0.633	0.679	0.588 0.588	0.612	0.629	18.45	0.9231	0.700	1.070	1.7148	1.737	0.067	-0.016
3,389	0.633	0,679		0.412	0.629	Ť	0.9231	0.700	1.070	1.7148	1.737	0.035	-0.010
0.889	0.625	0.670	0.576	014.0	0,419	18.45	0.9276	V.098	1.000	4.0724	1.770	0.050	0.026
0.734	0.649	0.631	0.624	0.623	0.612	15.50	0.8449	0.560	1.109	1.3139	1.812	0.033	0.034
0.734 0.883	0.652	0.717	0.601	0.623	0.673	20.572	0.8699	0.670	1.132	2.0215	1.817	0.055	0.003
	0.683	0.682	0.619	0.636	0.661	18,200	0.9664	u.680	1.195	1.6378	1.778	0.050	0.010
0.866 .: M58	0.650	0.650	0.610	0.619	0.640	19,685	0.8528	0.790	1.207	1.6843	1.601	0.055	0.049
9.858 9.863	0.599	0.661	0.575	0.607	0.616	22.500	0.8732	0.650	1.072	2.1333	1.697	0.017	0.028
7.863 3.8÷9	0.565	0.593	0.553	0.571	0.573	26,000	1.0217	0.706	1.227	2.2597	1.447	0.046	0.070
0.849	0.620	0.663	0.574	0.605	0.620	21,800	0.9943	0.710	1.060	2,2879	1.673	0.912	-0.012
0.885	0.619	9.663	0.618	0.644	0.620	23.800	0.9943	0.730	1.960	2.2879	1.650	9.049	406.0-
						1				ļ			
6. <b>88</b> 5	0.619	0.663	0.660	0,682	0.620	23.8	0.9943	0.730	1.960	2.2879	1.673	0.030	-0.010
2.882	J.659	0.660	0.593	0.593	0.660	20.372	0,9125	0.806	1.044	1.7687	1,636	0.035	-0.026
	0.633	0.679	0.584	0.612	0.629	13.0	1.0384	0.791	1.037	1.5131	1.277	0.051	-0.011
5.889	0.613	0.679	0.655	0.674	0.629	13,0	1.0384	0.741	1.037	1.5131	1.277	9.060	0.017
3.875	0.573	0.603	0.512	0.558	0.563	23.942	0.8889	0.730	1.060	2.2584	1.581	0.037	0.020
2.875	0.571	9.503	0.540	0.565	0.563	21.942	0.6889	0.730	1,060	2.2584	1.581	0,066	-0.003
5.876	0.568	0.605	0.531	0.557	0.565	23,942	0.8889	0.485	1.983	2.2584	1.581	0.060	-0.005
0.871	0.558	0.657	0.616	0.528	0.644	21.524	0.9000	0.686	1.105	1.8251	1.610	0.934	-0.016
214.3	2.070		2.310	,,,				3"					
0.873	0.658	9.657	9.632	0.643	0.644	21.524	0.9000	0.679	1.146	1.8251	1.610	0.041	100.00
0.872	0.577	9.604	0.561	0.561	0.609	22,796	0.8182	0.816	1.369	2.2162	1,461	0.086	-0.915
0.897	0.575	0.614	0.563	0.601	0.569	24.064	0.8108	0.675	1.047	2.1333	1.291	0.080	0.033
.897	0.575	0.614	0.576	0,613	0.569	24,064	0.8108	0.625	1.047	2.1933	1.291	0.105	0.038
0.894	0.398	0.654	0.557	0.578	0.611	22.706	0.7447	9.765	0.952	2.0725	1.310	0.100	0.030
9.894	0.198	0.654	0.584	0.601	0.633	22,706	0.7447	0.765	0,952	2.0725	1.410	9.026	0.046
0.907	9.510	0.643	0.617	0.629	0.679	24.064	0.7389	0.675	1.047	2.0687	1.246	0.094	0,030
G.880	0.608	0.594	0.569	0.591	0,559	24.064	0.7317	0.675	1.047	2.2913	1.184	0.101	0.049
0.931	0.586	0.655	0.651	0.671	0.612	23.8	1.0102	0,730	1,060	2.2879	1.670	0.021	-0.002
0.901	0.616	9.630	0.501	0.619	0.609	24.064	0.7317	0.675	1.047	2.2518	1.257	0.072	0.019
U.884	0.564	0.642	9.545	0.563	0.585	25.511	9.8767	0.686	1.105	2.2123	1.397	0.065	0,004
5.961	0.559	0.597	0.349	0.579	0.541	24.636	0.9167	0.615	1.021	2.1155	1.335	0.060	-0.002
9.962	0.580	0.640	9.402	0.615	9.614	75.512	0.9697	0.679	1.146	• .	1.399	0.080	-0.002
0.960	0.581	0,649	9.575	0.590	0.626	25.512	0,9357	0.679	1.146	1.8184	1.198	0.104	-0.013
9.966	0,583	0.644	0.575	9,590	0.626	25.512	0.9357	0.679	1.146	1.8184	1.398	0.080	-0.001
0.861	0.586	0.606	0.578	0.578	0.606	25.500	0.9457	0.726	1.175	1.9753	1.142	0.066	0,000
						}							
6.931	0.518	9.673	0.597	0.631	0.614	24.064	0.7317	0.675	1.047	2.2123	1.268	0.068	0.033
0.917	0. 162	9.628	0.345	0.576	0.574	24.824	0.8718	0.575	1,457	2.0946	1.303	0.062	9.037
0.917	0,542	0.628	9.545	0.576	0.574	74.874	0.8/18	0.575	1.457	2.0946	1.303	0.050	0.012
0.881	0.628	Ď. <del>1</del> 59	0.196	0.614	0.639	24.824	1.0119	0.5/5	1.457	1.9290	1.358	0.085	0.012
0.473	0.622	(1.659	9.579	0.514	0.617	15,000	0.8500	0.461	0.892	0.9481	1,386	0.055	0,005
0.71)	0,656	0.672	O.AZR	0.677	0.624	22.143	0.9574	0.595	1.102	1.2286	1.704	0.215	0.121
r. 853	9.611	0.661	0.574	0.612	0.620	16.700	1.0121	0.830	1,080	1,5834	1.970	บางร	-0.049
9 <b>8</b> 53	0.631	0.661	0.514	0.617	0.620	16.700	1.0127	0.630	1.080	1.5834	1.970	0.060	0.014
9.871	0.522	0.641	9,564	0.594	0.590	18,600	0.9218	0.640	1.170	1.7145	1.815	0.055	0.045

## PRECEDING PACE BLANK-NOT FILMED

## APPENDIX C

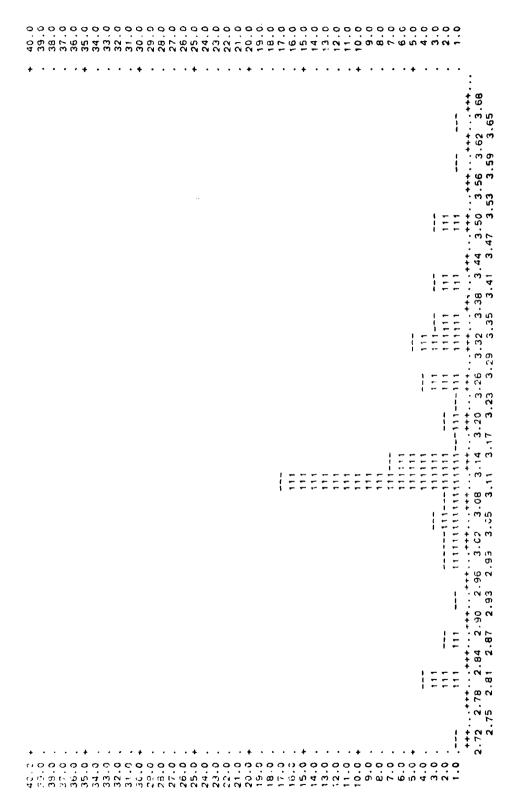
FREQUENCY DISTRIBUTION OF INDEPENDENT AND DEPENDENT VARIABLES FOR TWIN-SCREW DESTRYOYERS

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Figure C-1 - Frequency Distribution of the Wetted Surface Coefficient for Twin-Screw Destroyers

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Figure C-2 - Frequency Distribution of the Length-Beam Ratio for Twin-Screw Destroyers



- Frequency Distribution of the Beam-Draft Ratio for Twin-Screw Destroyers Figure C-3

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Figure C-4 - Frequency Distribution of the Prismatic Coefficient for Twin-Screw Destroyers

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Figure C-5 - Frequency Distribution of the Half Angle of Entrance for Twin-Screw Destroyers

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Figure C-6 - Frequency Distribution of the Longitudinal Center of Buoyancy-Waterline Length Ratio for TWin-Screw Destroyers

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Figure C-7 - Frequency Distribution of Taylor's 'f' for Twin-Screw Destroyers

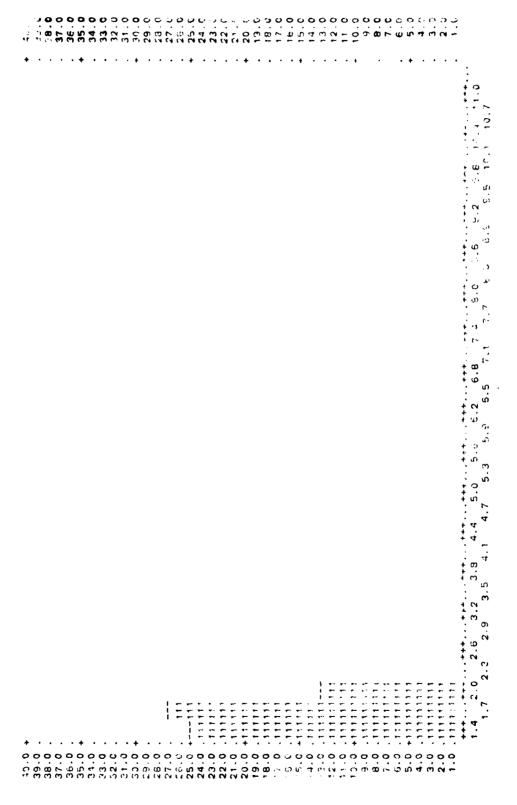


Figure C-8 - Frequency Distribution of the Fatness Ratio for Twin-Screw Destroyers

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Figure C-9 - Frequency Distribution of the Waterplane Coefficient for Twin-Screw Destroyers

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Figure C-10 - Frequency Distribution of the Longitudinal Center of Flotation-Waterline Length Ratio for Twin-Screw Destroyers

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Figure C-11 - Frequency Distribution of the Length of Parallel Middlebody-Waterline Length Ratio for Twin-Screw Destroyers

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Figure C-12 - Frequency Distribution of the Length of Entrance-Waterline Length Ratio for Twin-Screw Destroyers

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Figure C-13 - Frequency Distribution of the Afterbody Waterplane Coefficient for Twin-Screw Destroyers

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Figure C-14 - Frequency Distribution of the Forebody Waterplane Coefficient for Twin-Screw Destroyers

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Figure C-15 - Frequency Distribution of the Afterbody Prismatic Coefficient for Twin-Screw Destroyers

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Figure C-16 - Frequency Distribution of the Forebody Prismatic Coefficient for Twin-Screw Destroyers

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Figure C-17 - Frequency Distribution of the Entrance Prismatic Coefficient for Twin-Screw Destroyers

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Figure C-18 - Frequency Distribution of the Run Prismatic Coefficient for Twin-Screw Destroyers

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Figure C-19 - Frequency Distribution of the Scale Ratio for Twin-Screw Destroyers

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Figure C-20 - Frequency Distribution of the Propeller Diameter-Draft Ratio for Twin-Screw Destroyers

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Figure C-21 - Frequency Distribution of the Projected Area-Disk Area Ratio for Twin-Screw Destroyers

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Figure C-22 - Frequency Distribution of the Pitch Ratio for Twin-Screw Destroyers

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Figure C-23 - Frequency Distribution of the Ship Reynolds Number for Twin-Screw Destroyers

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Figure C-25 - Frequency Distribution of the Thrust. Deduction Fraction for Twin-Screw Destroyers

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Figure C-26 - Frequency Distribution of the Thrust-Wake Fraction for Twin-Screw Destroyers

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## APPENDIX D

VARIATION OF INDEPENDENT VARIABLES
WITH THRUST-DEDUCTION AND THRUST-WAKE FRACTIONS

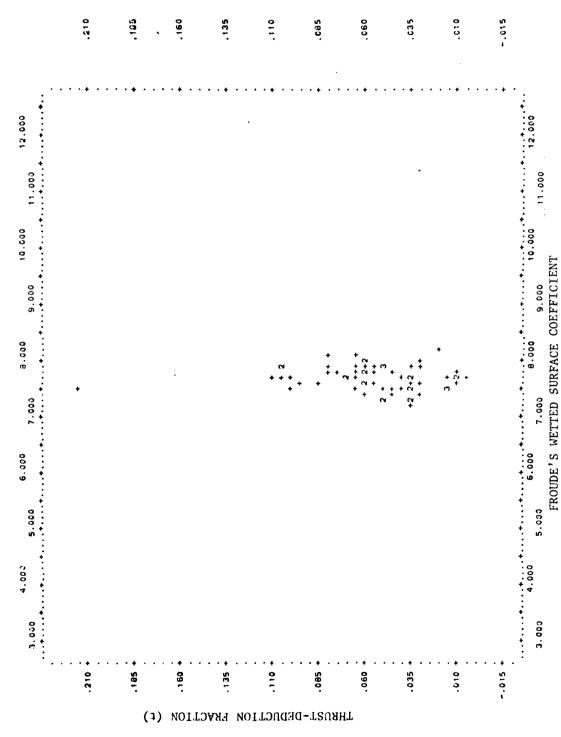


Figure D-1 - Variation of Froude's Wetted Surface Coefficient and Thrust-Deduction Fraction

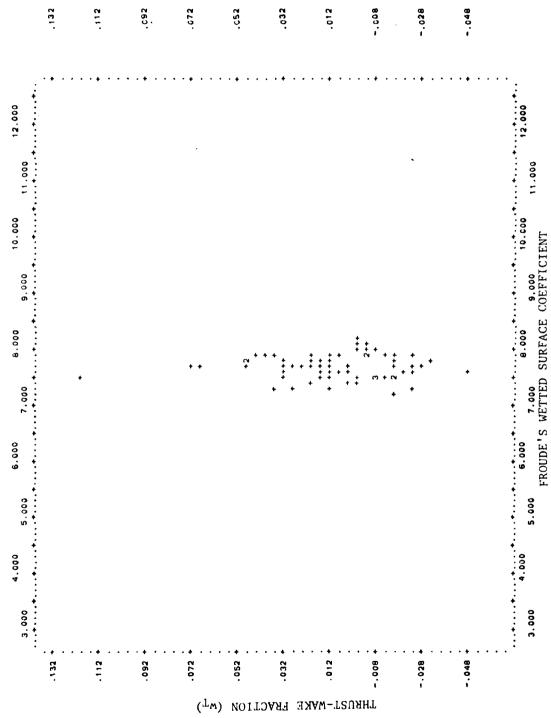


Figure D-2 - Variation of Froude's Wetted Surface Coefficient and Thrust-Wake Fraction

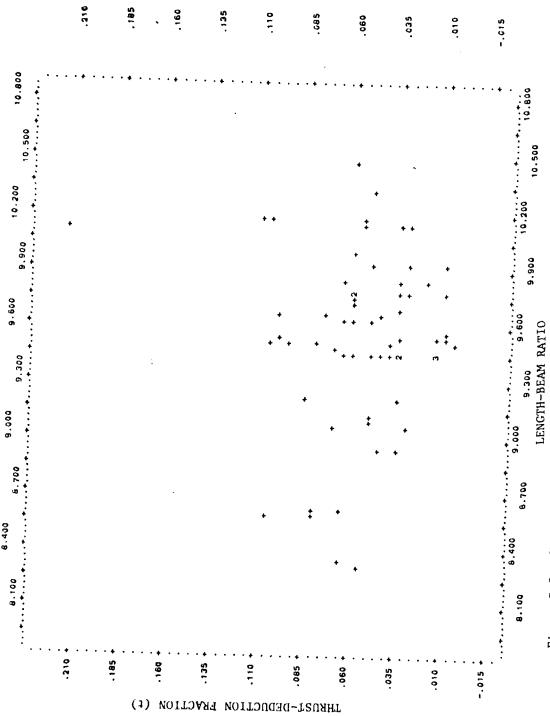
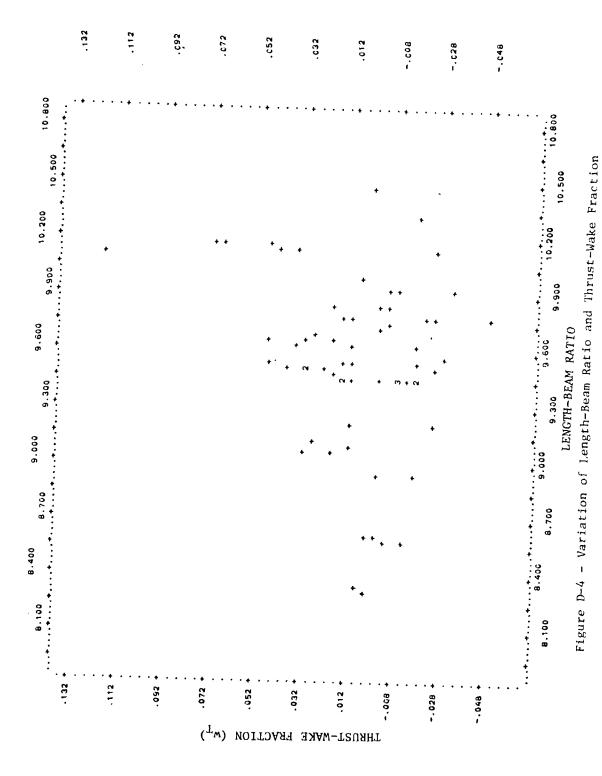
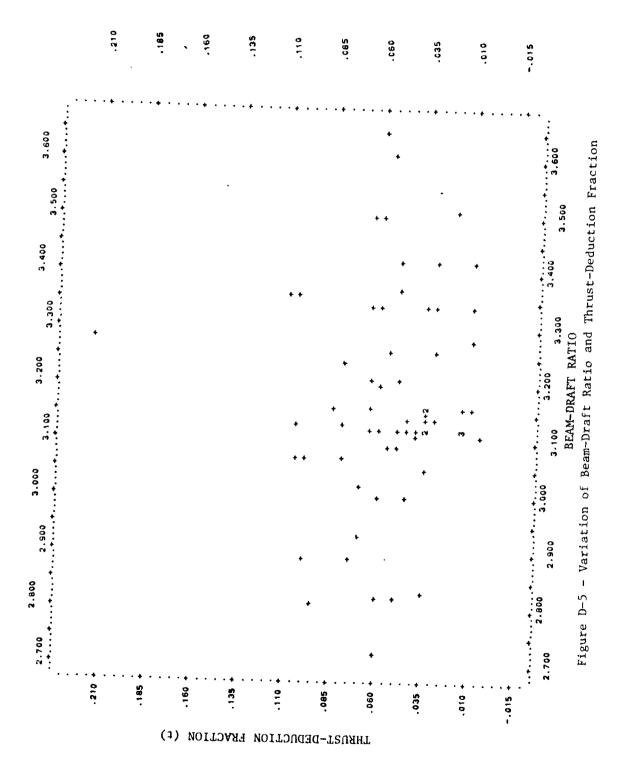


Figure D-3 - Variation of Length-Beam Ratio and Thrust-Deduction Fraction





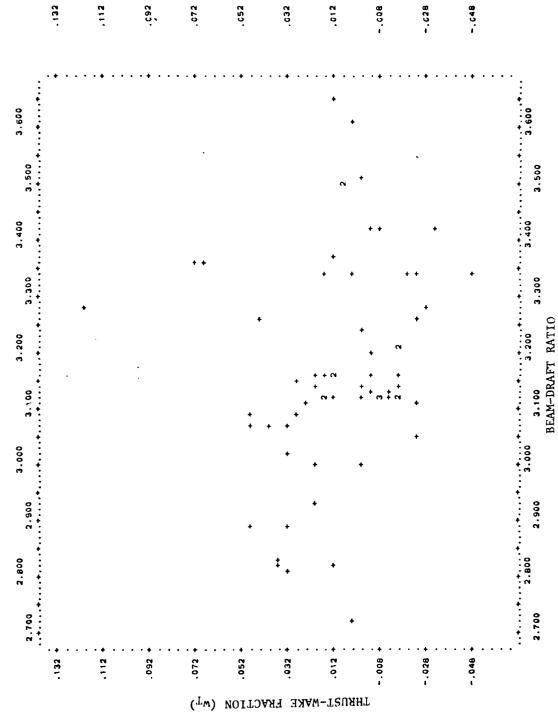
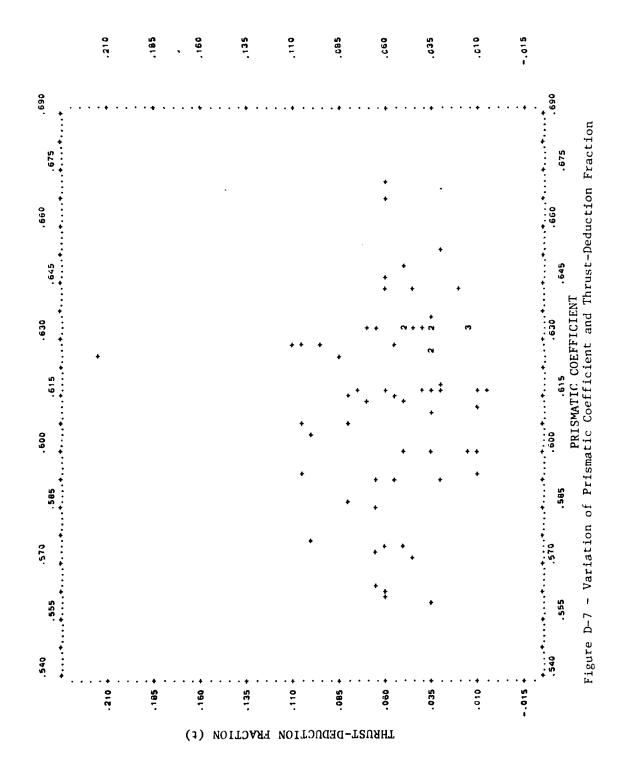
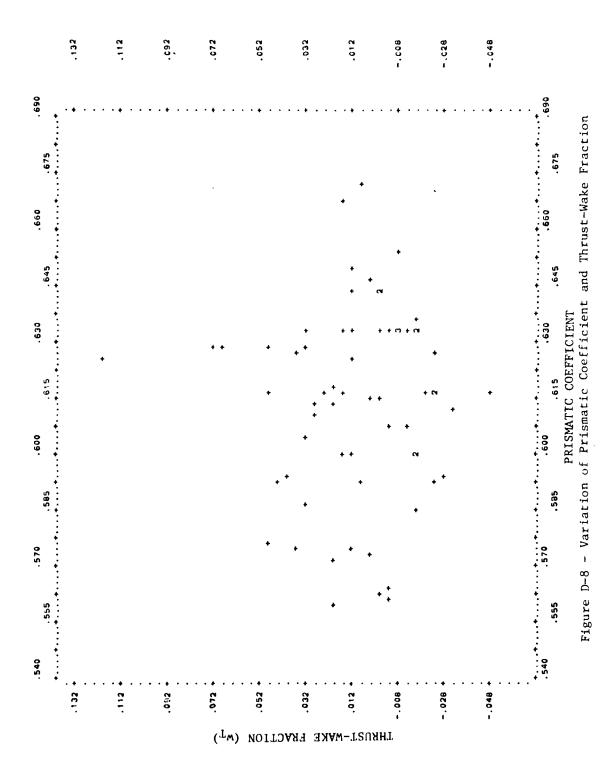
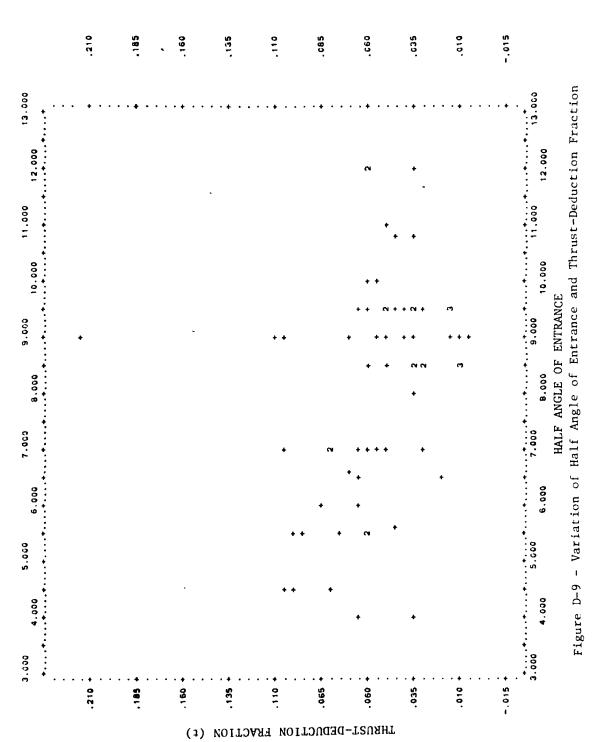
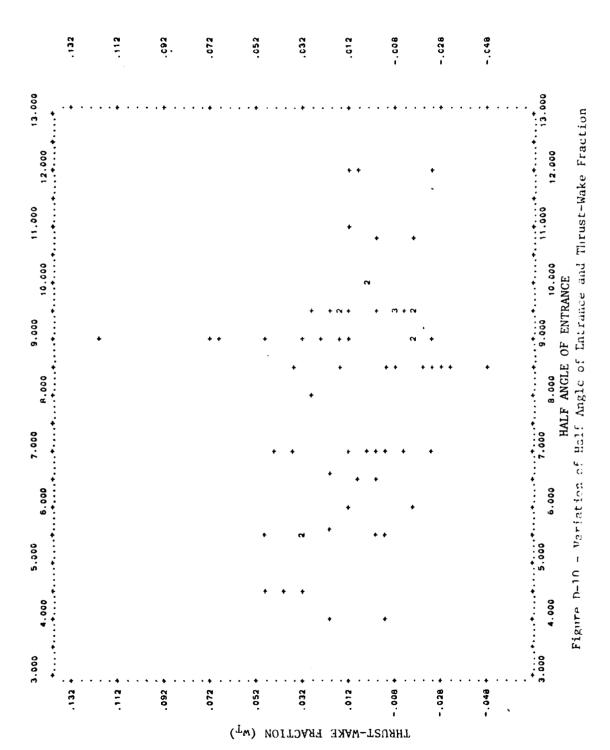


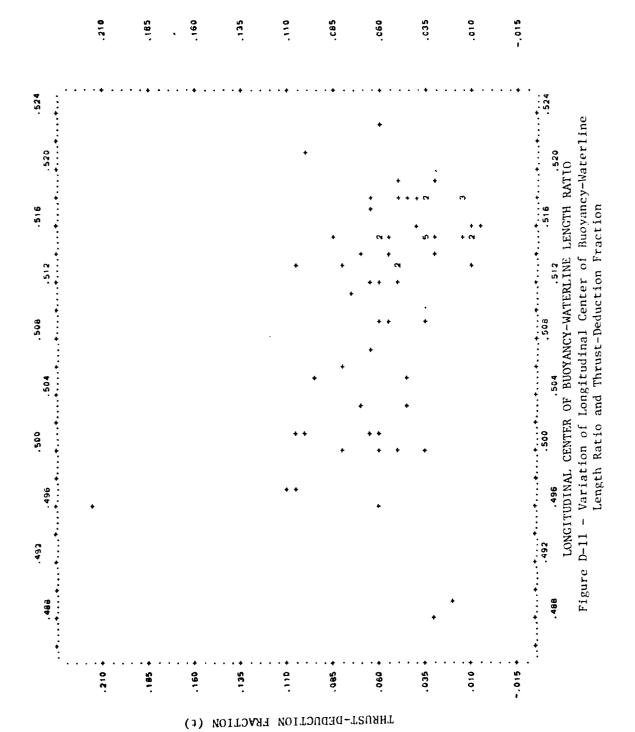
Figure D-6 - Variation of Beam-Draft Ratio and Thrust-Wake Fraction

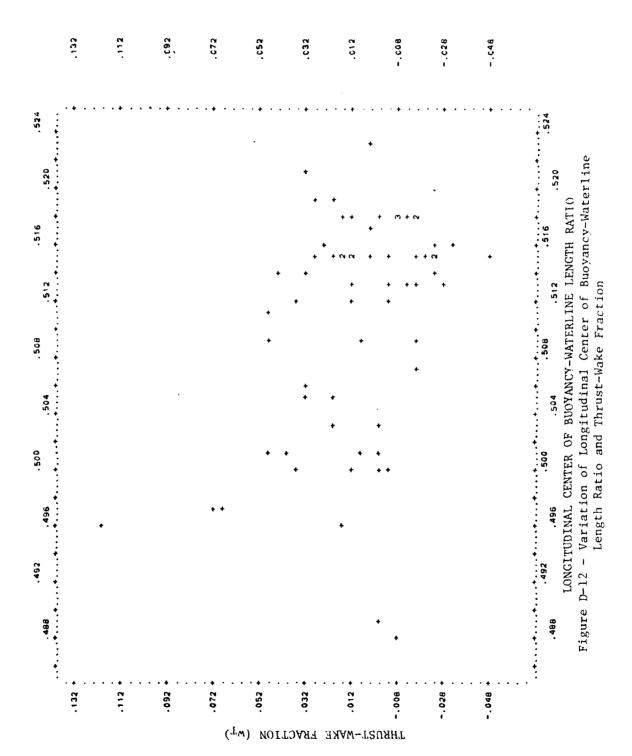


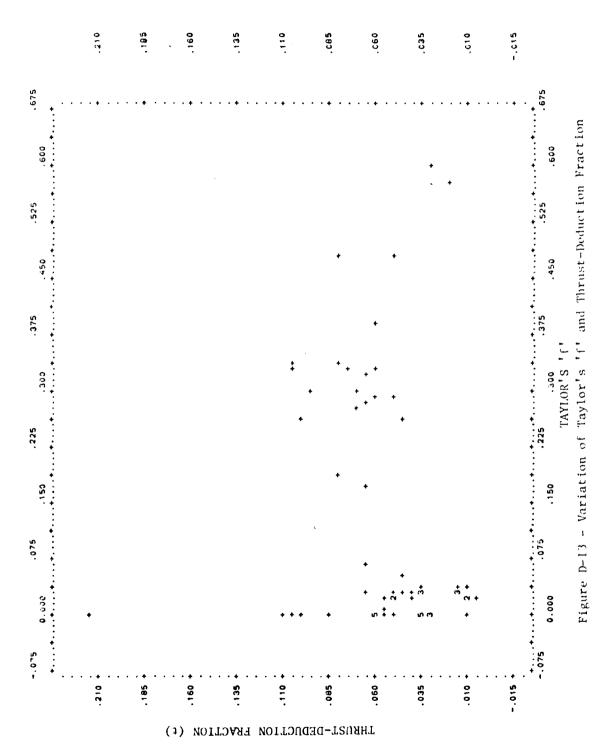


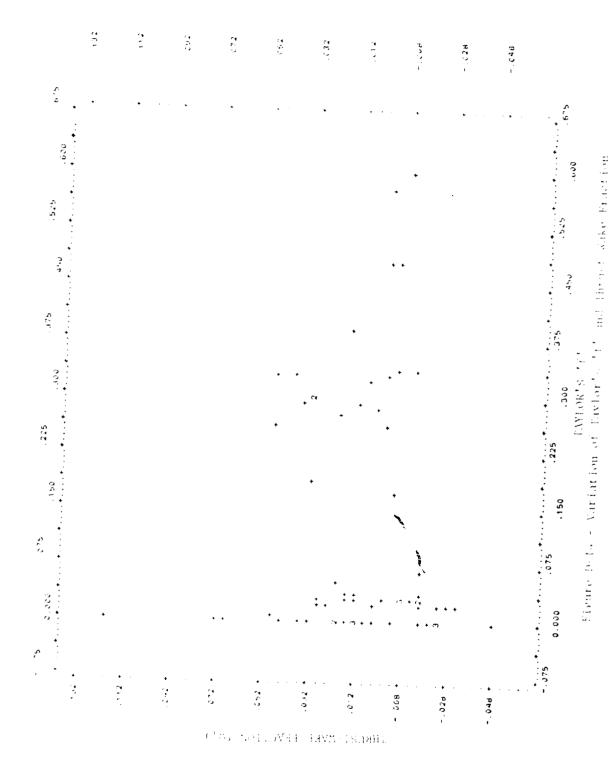


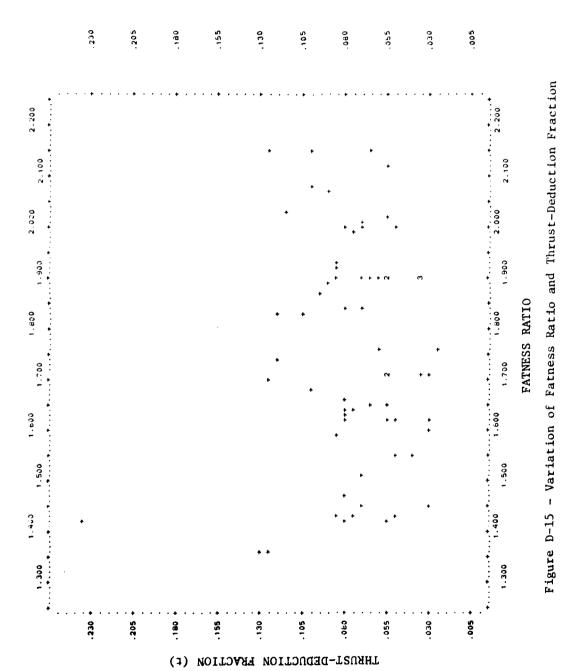












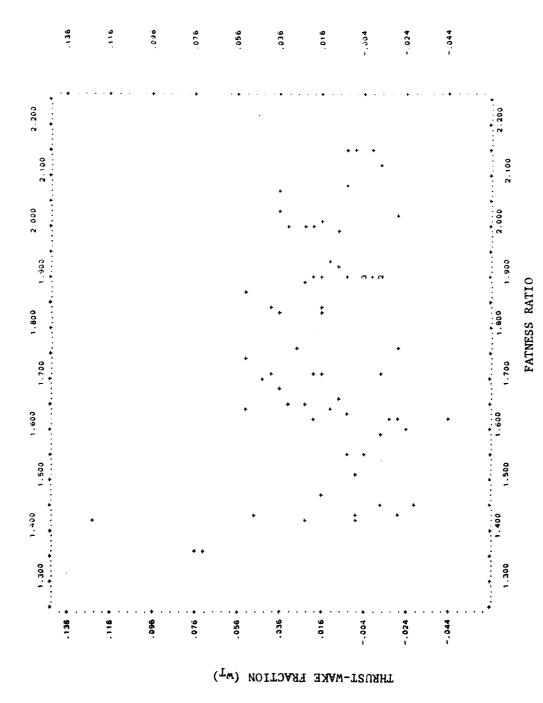
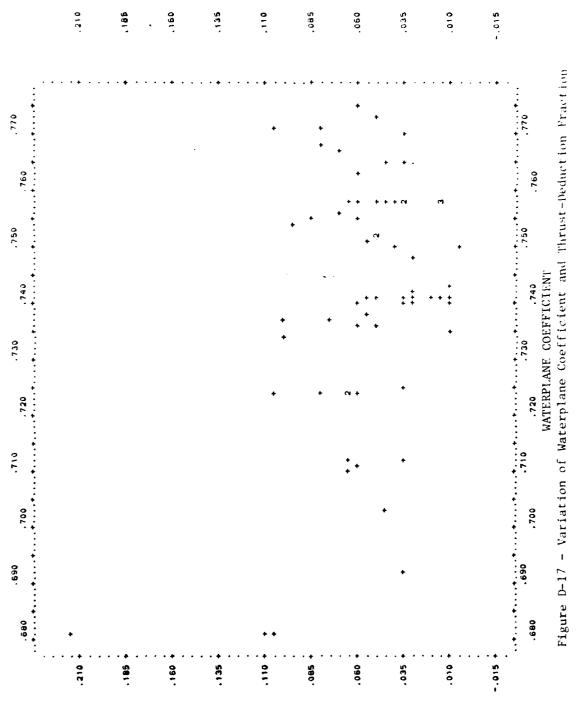
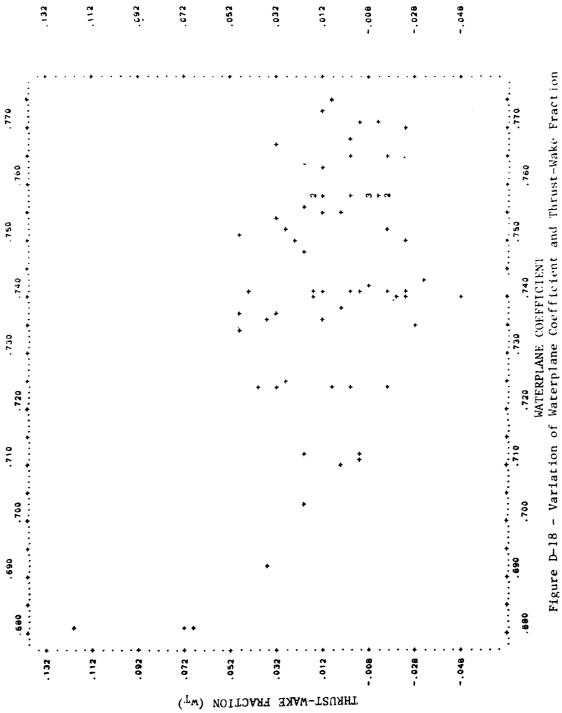
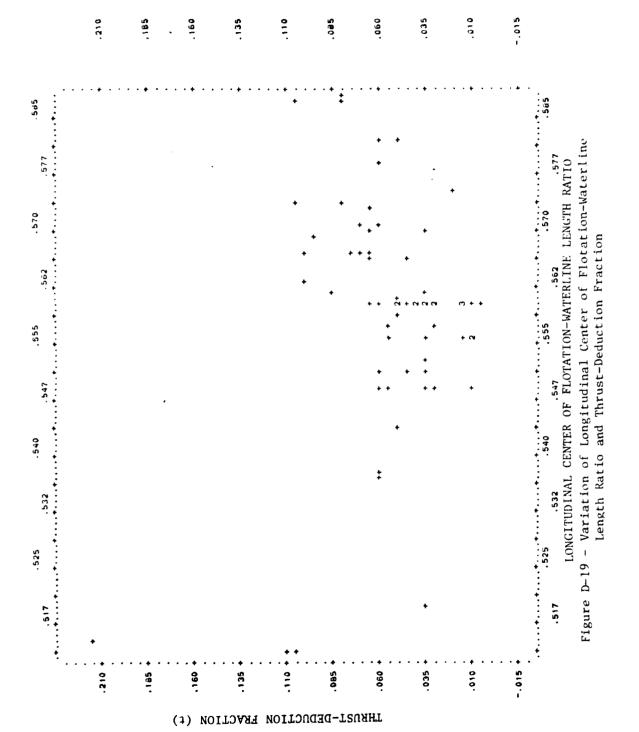


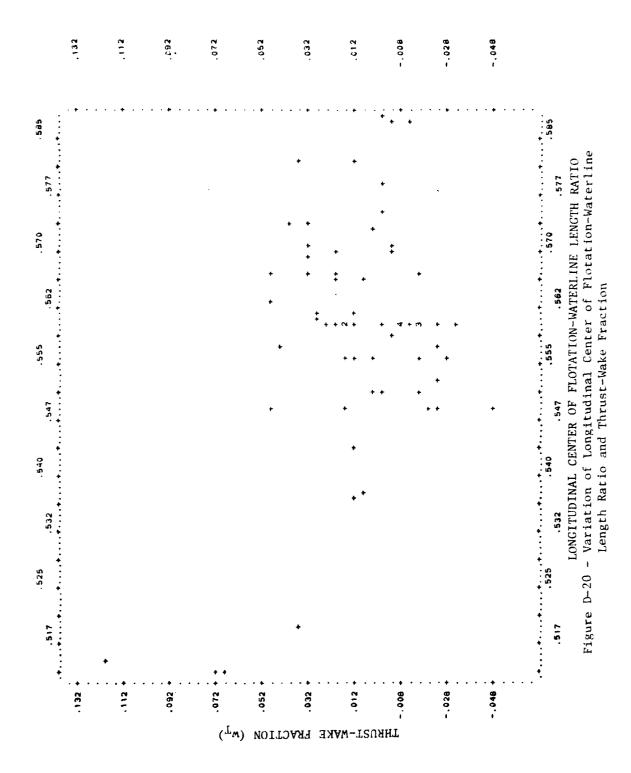
Figure D-16 - Variation of Fatness Ratio and Thrust-Wake Fraction

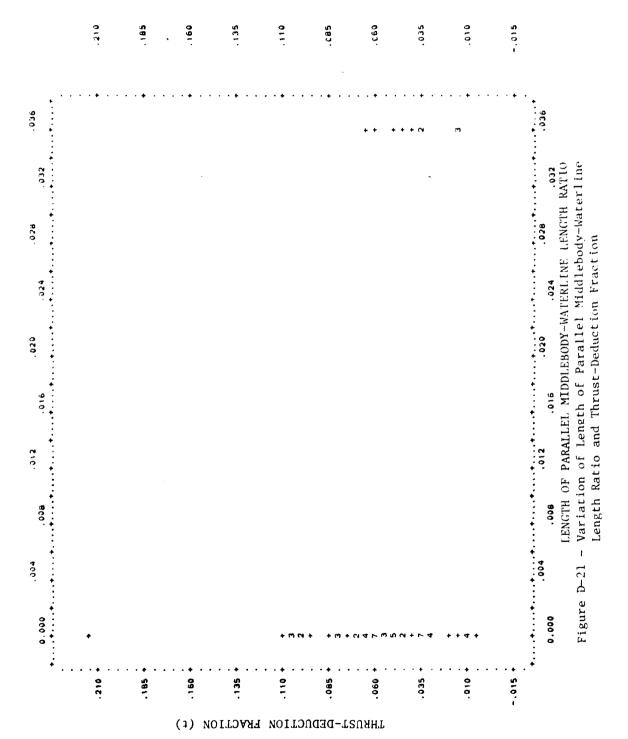


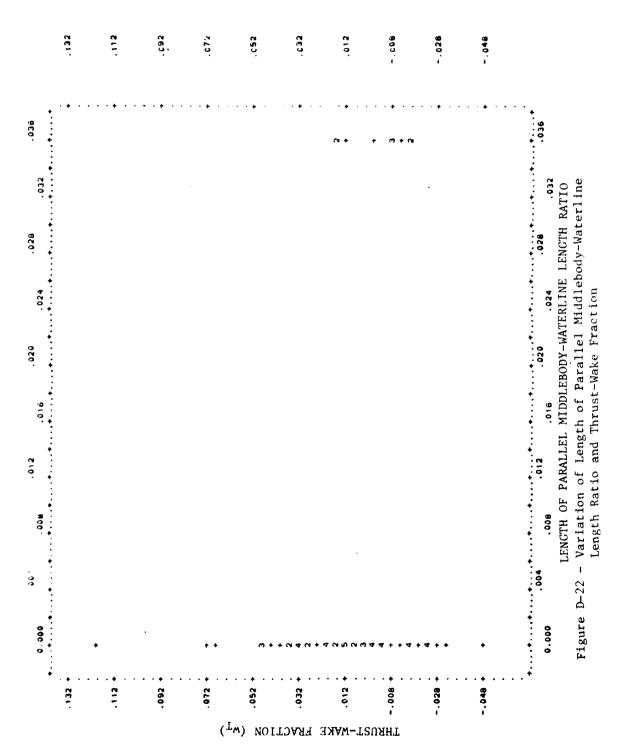
THRUST-DEDUCTION FRACTION (1)

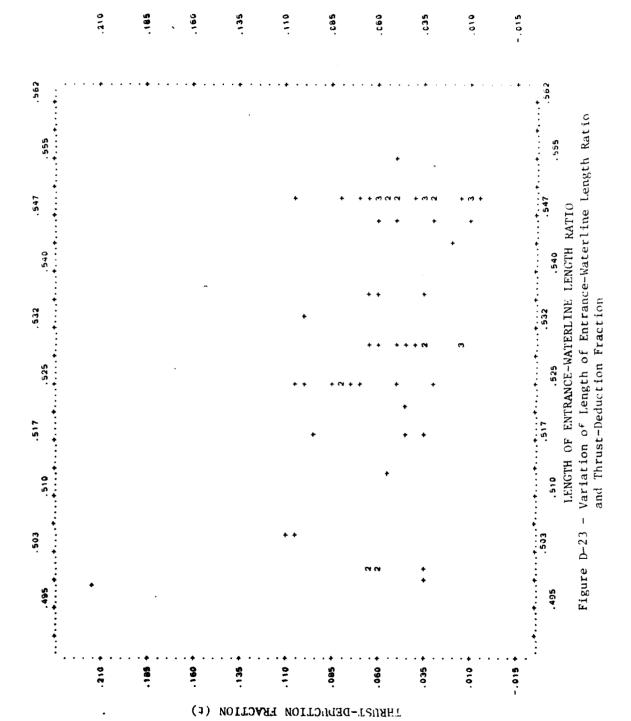


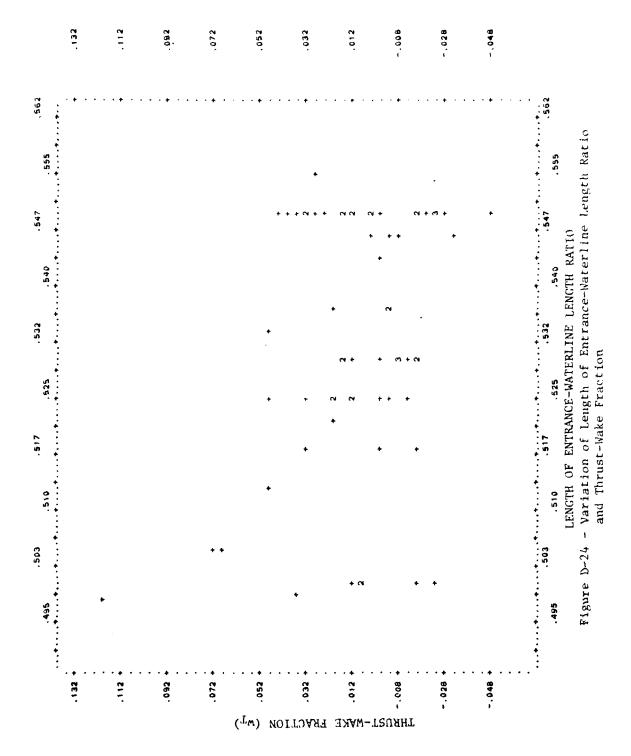


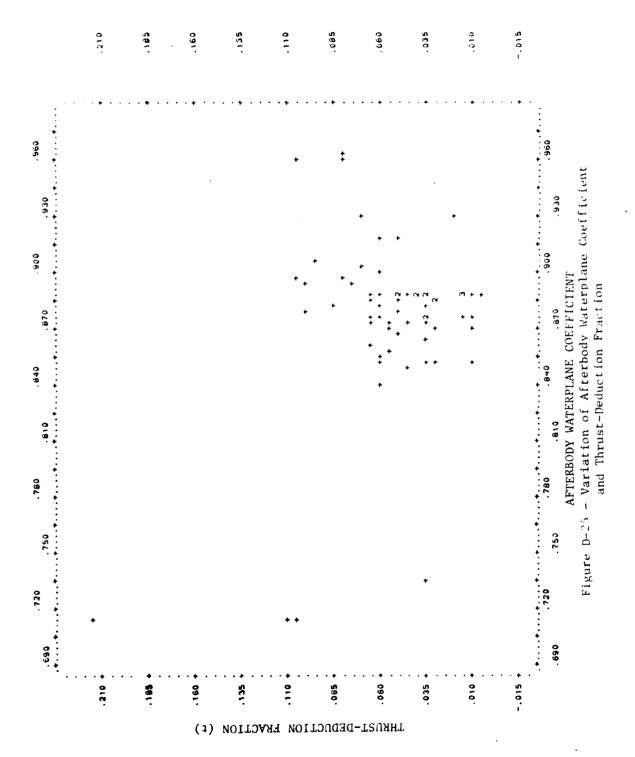


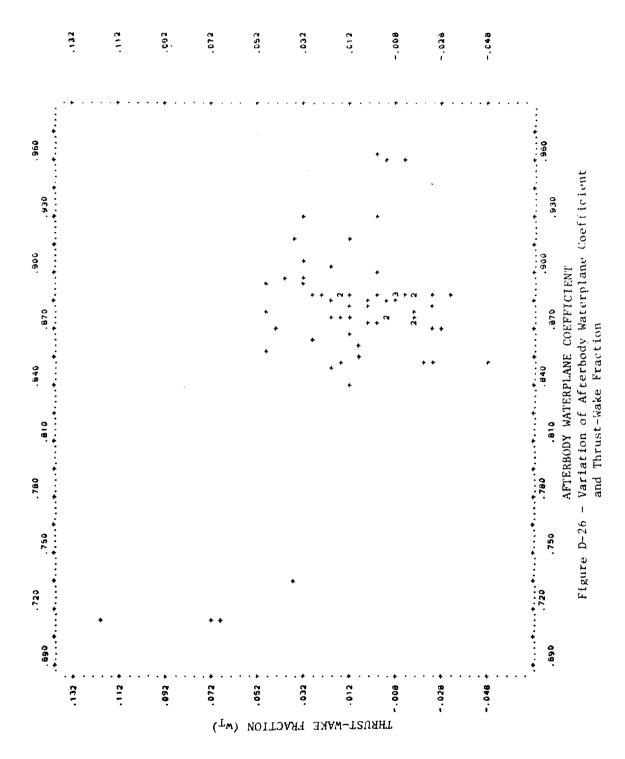


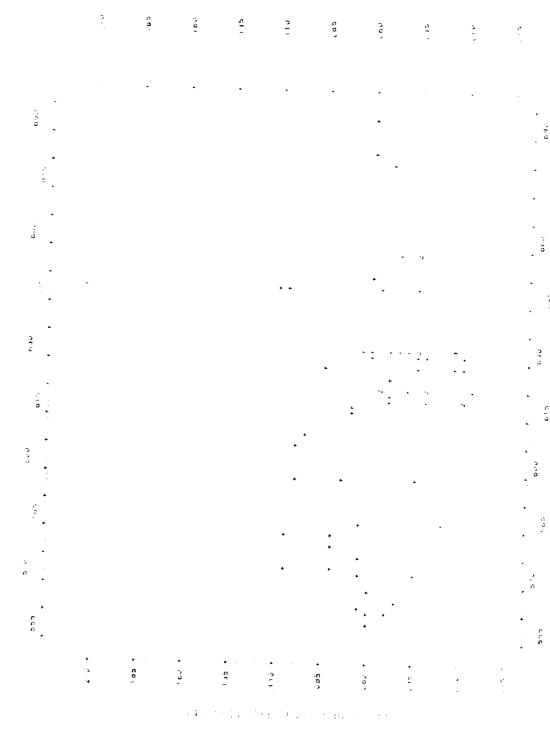




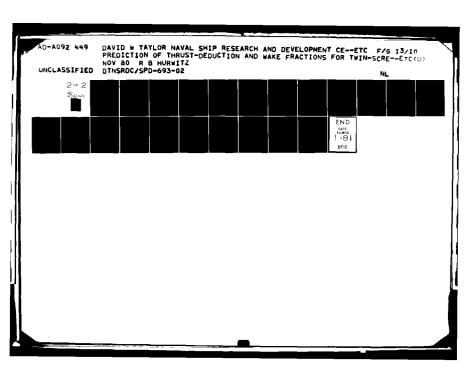


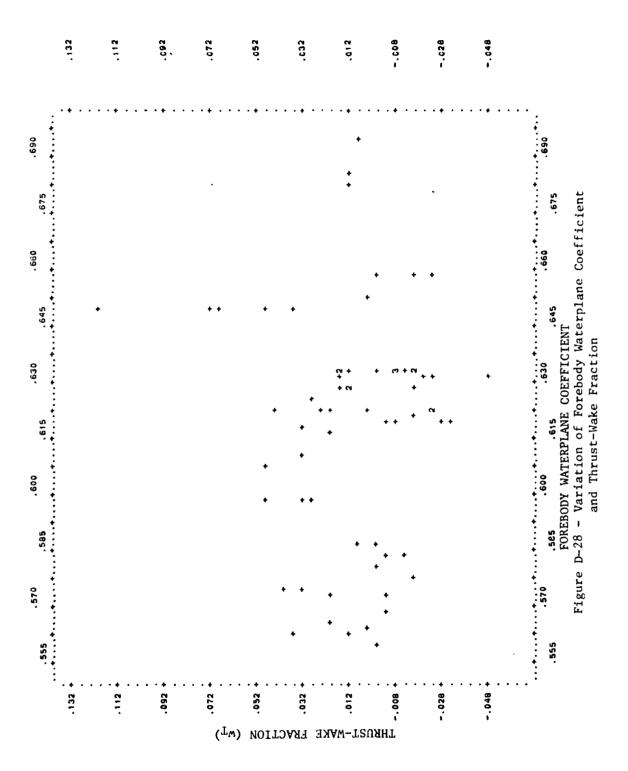


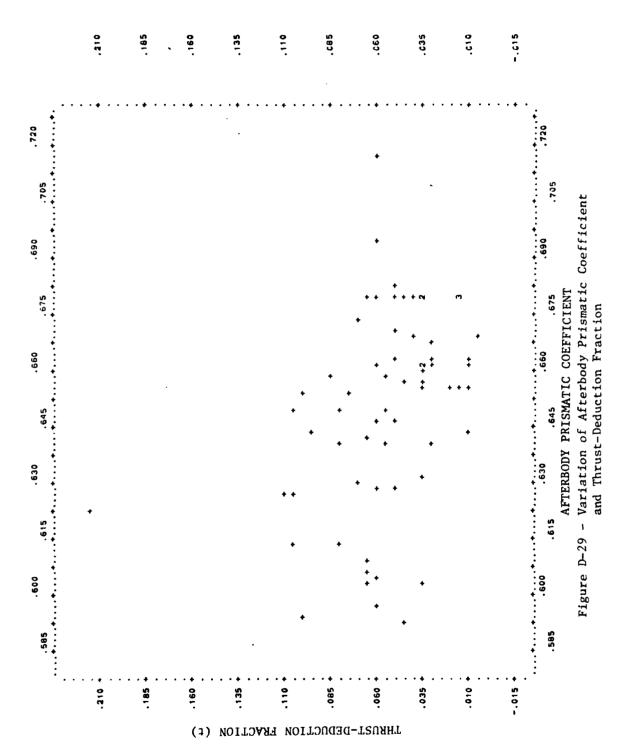


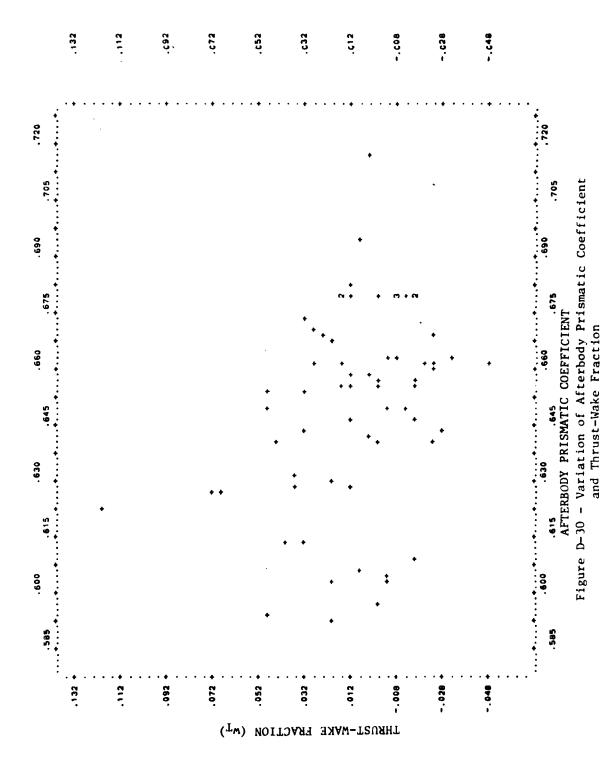


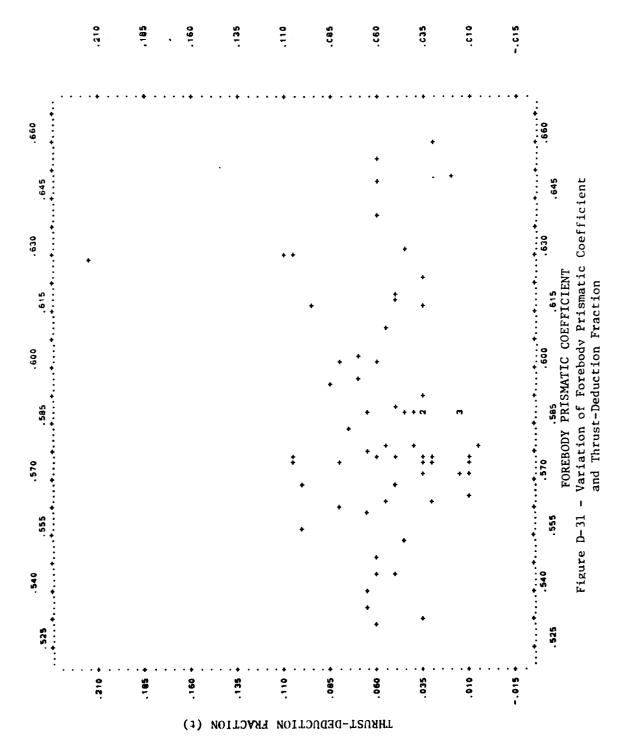
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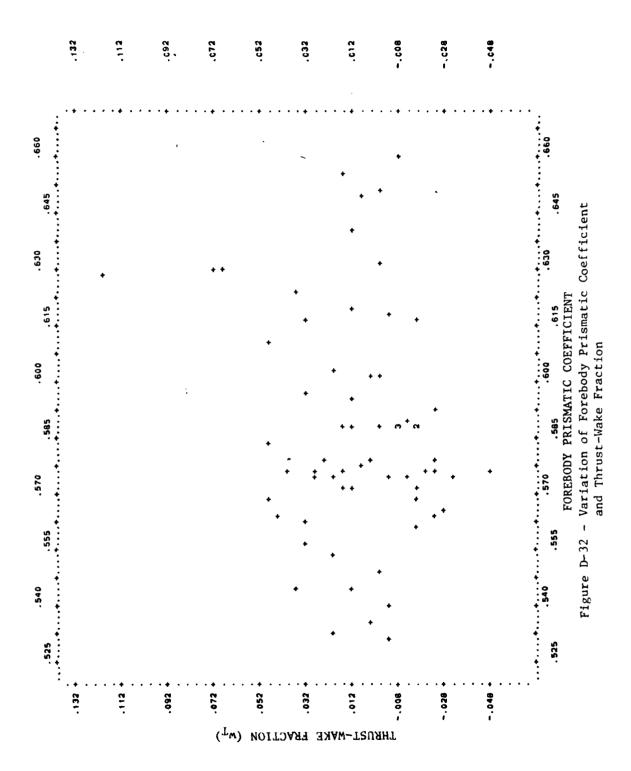


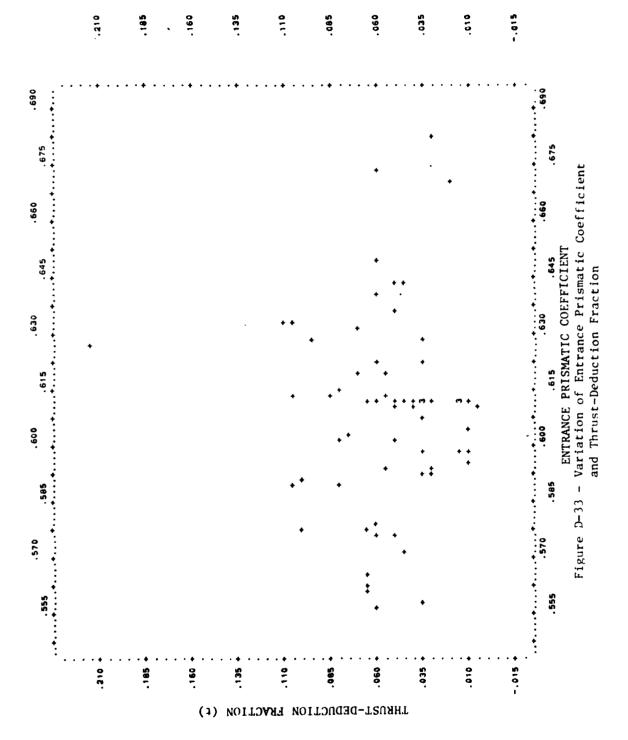


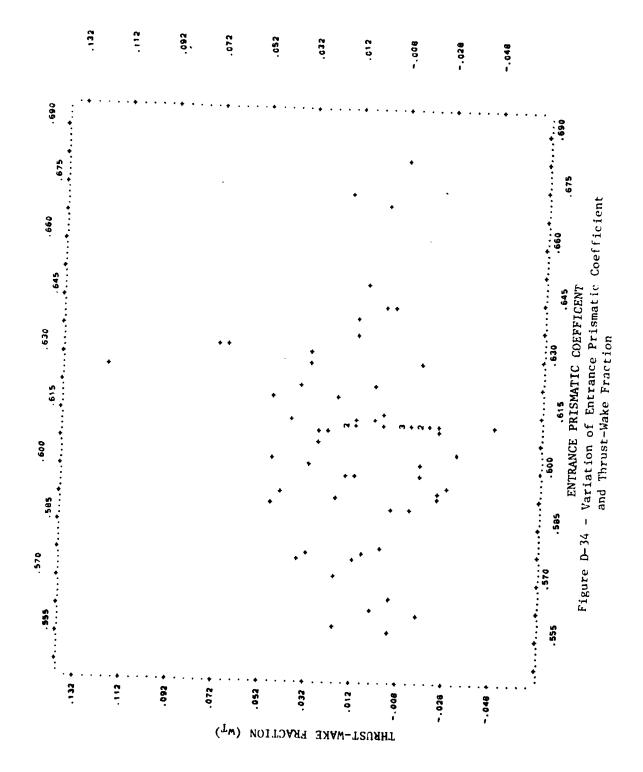


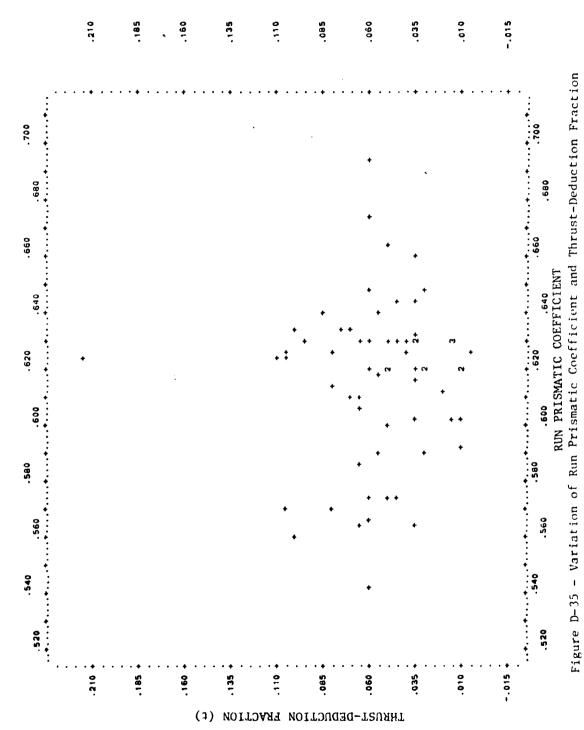












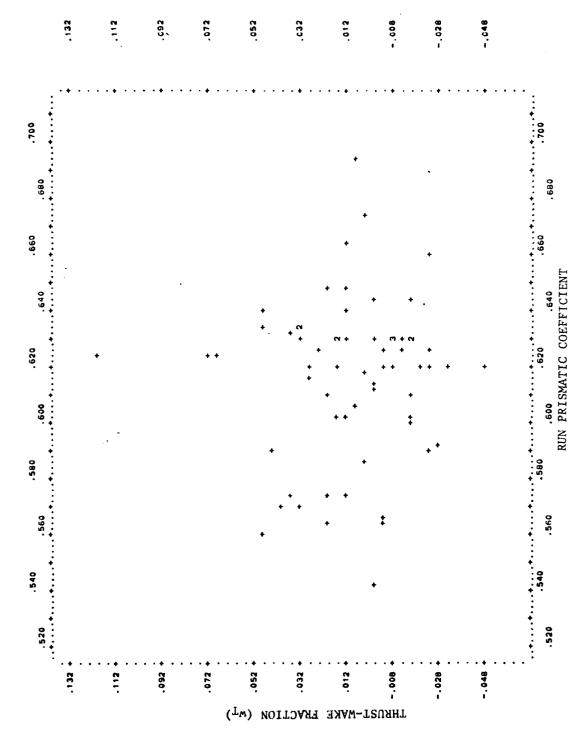


Figure D-36 - Variation of Run Prismatic Coefficient and Thrust-Wake Fraction

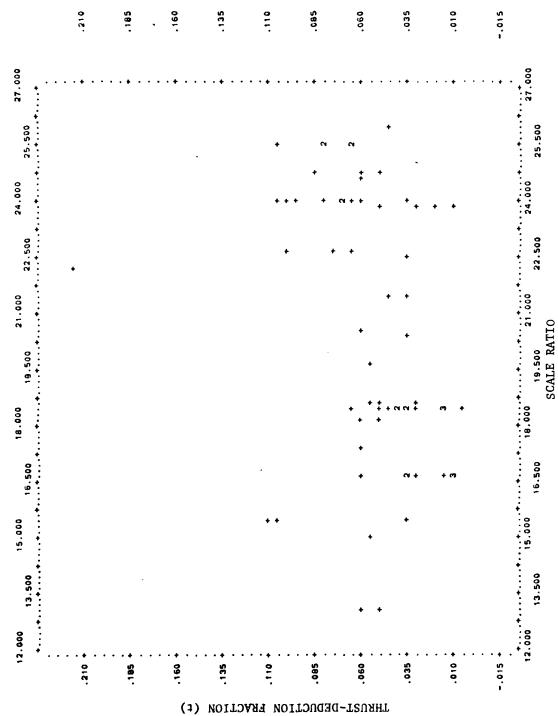
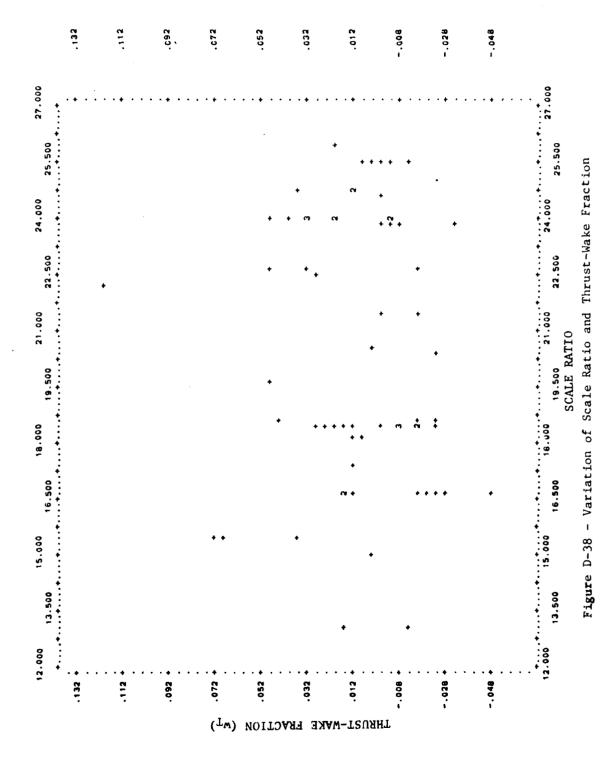
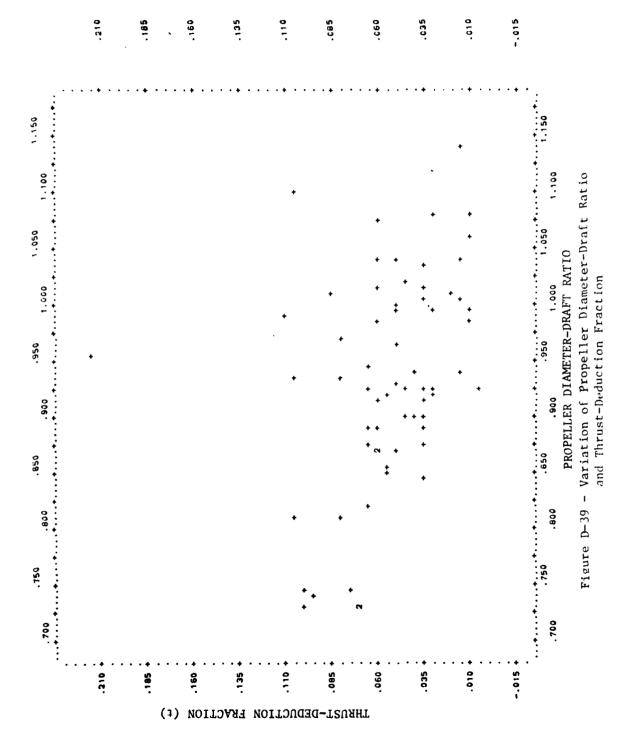
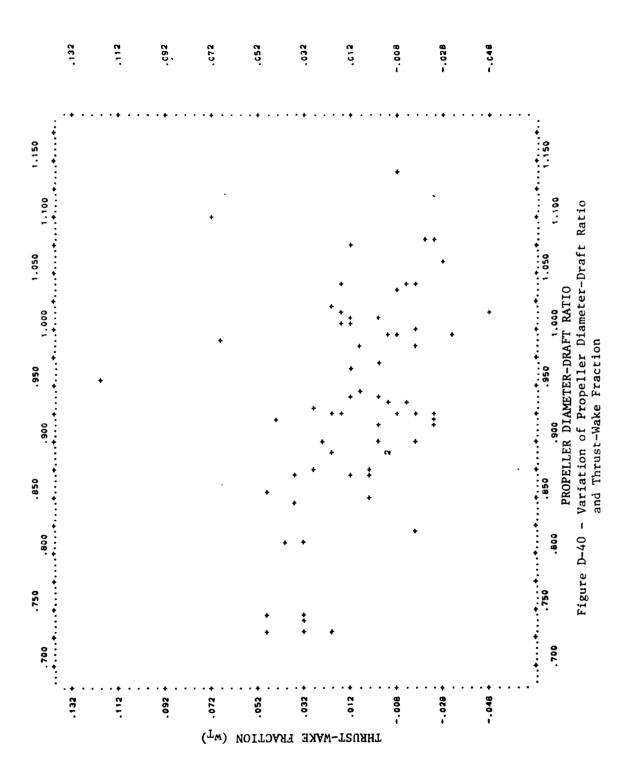
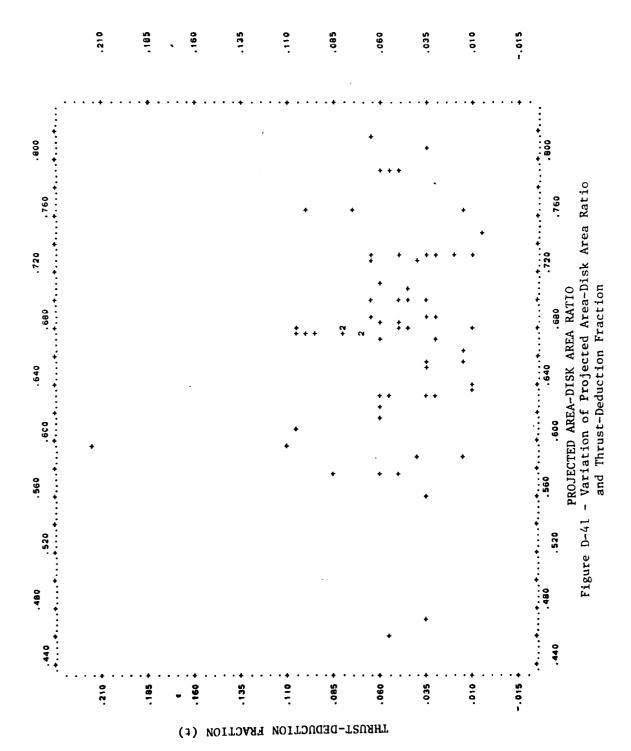


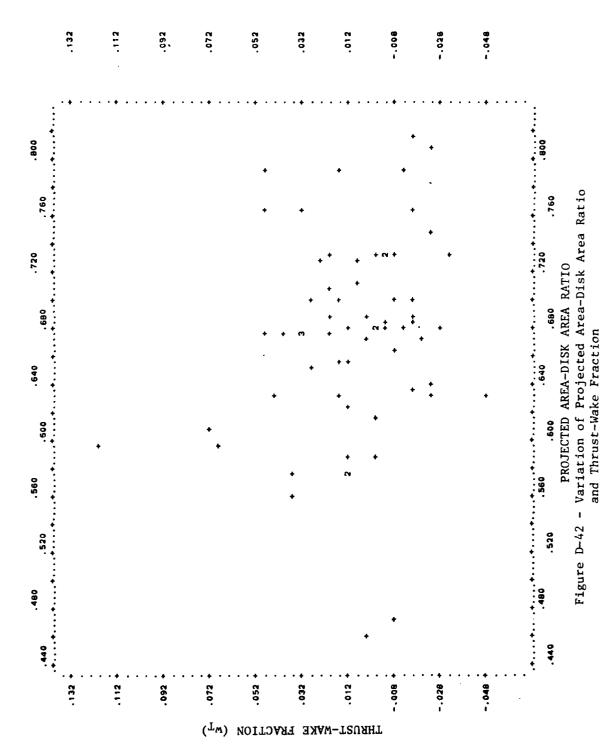
Figure D-37 - Variation of Scale Ratio and Thrust-Deduction Fraction

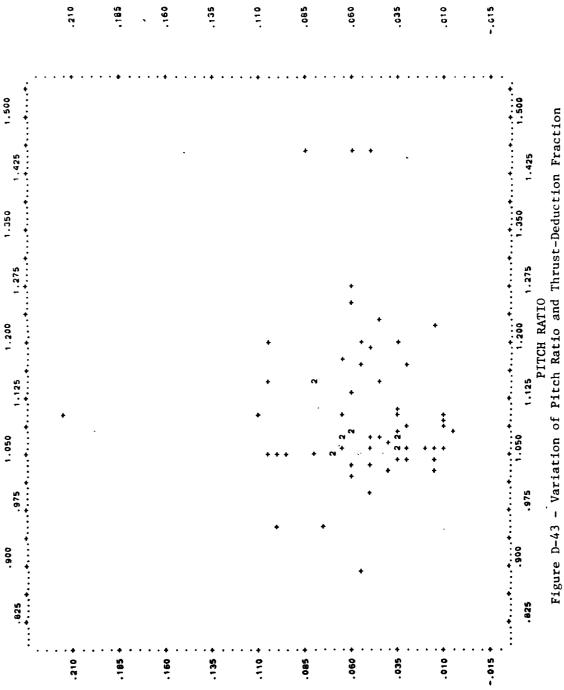












THRUST-DEDUCTION FRACTION (t)

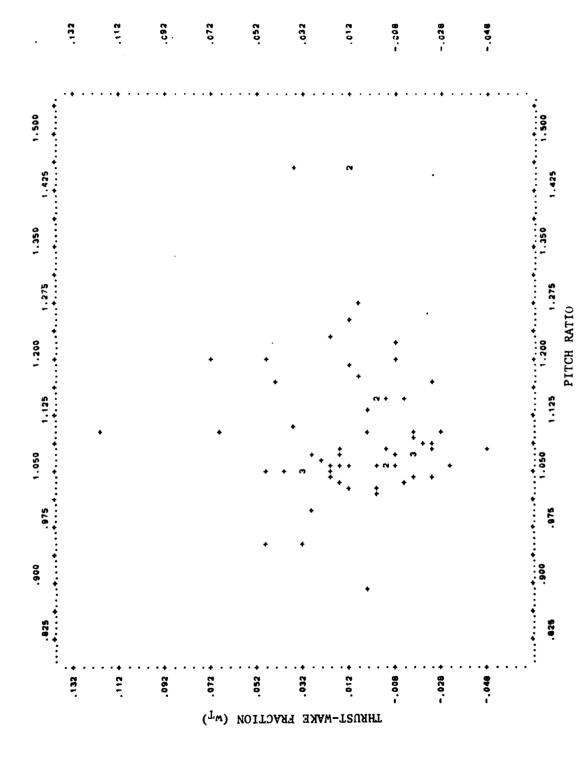
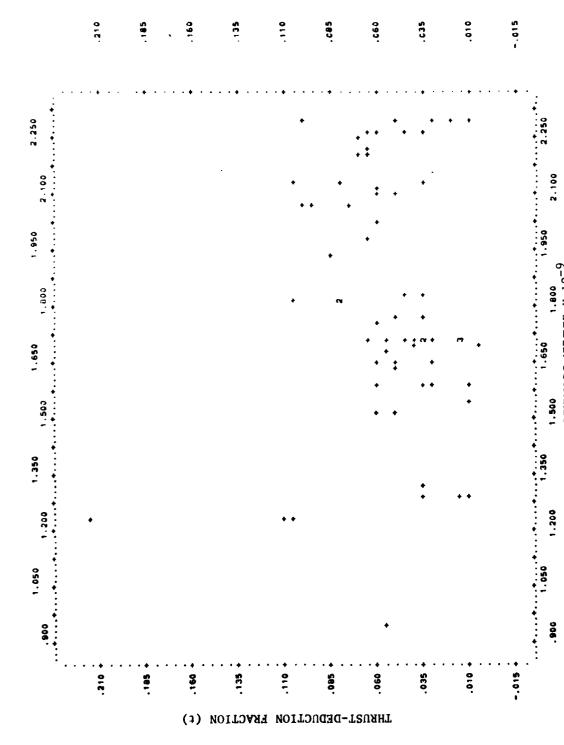
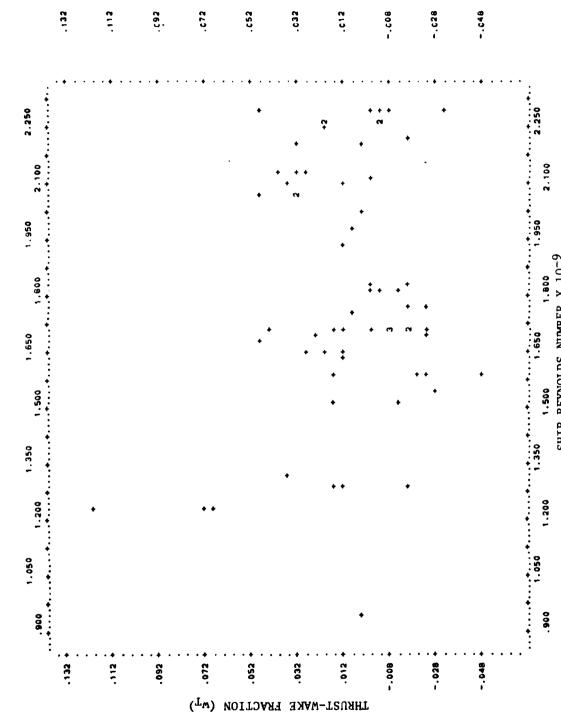


Figure D-44 - Variation of Pitch Ratio and Thrust-Wake Fraction



SHIP REYNOLDS NUMBER X 10<sup>-9</sup>
Figure D-45 - Variation of Ship Reynolds Number and Thrust-Deduction Fraction



SHIP REYNOLDS NUMBER X  $10^{-9}$  Figure D-46 - Variation of Ship Reynolds Number and Thrust-Wake Fraction

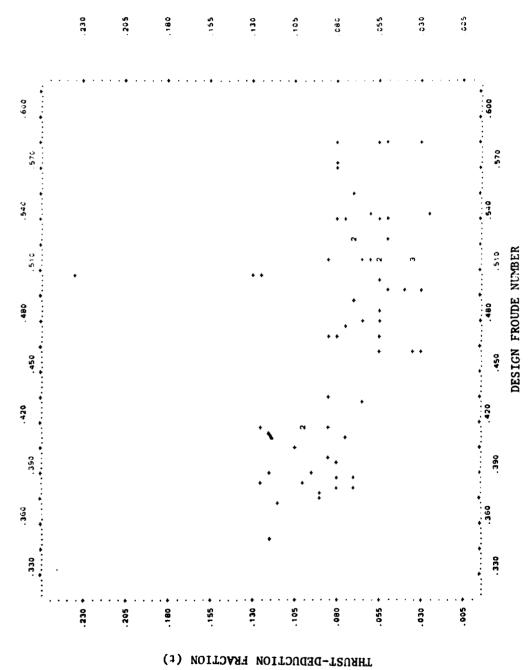


Figure D-47 - Variation of the Design Froude Number and Thrust-Deduction Fraction

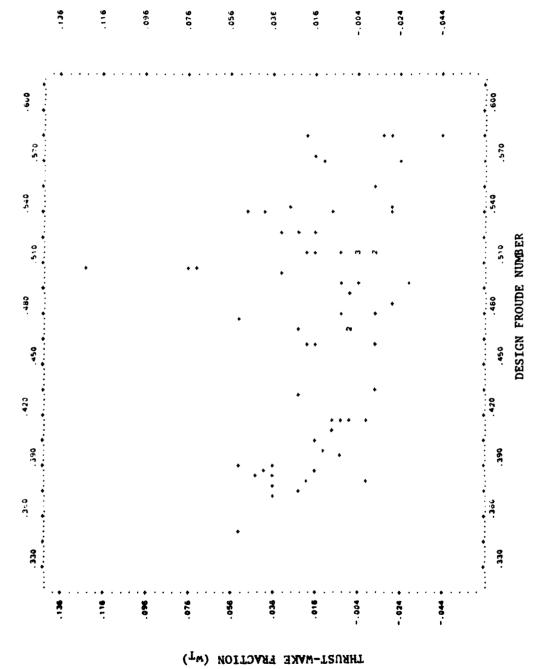


Figure D-48 - Variation of the Design Froude Number and Thrust-Wake Fraction

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